

Fundamentals of Power Electronics

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Dedicated to

Linda and William

Robert Sr., Pearlie, and Karen

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