Attia, John Okyere. "Two-Port Networks." *Electronics and Circuit Analysis using MATLAB*. Ed. John Okyere Attia Boca Raton: CRC Press LLC, 1999

#### **CHAPTER SEVEN**

## **TWO-PORT NETWORKS**

This chapter discusses the application of MATLAB for analysis of two-port networks. The describing equations for the various two-port network representations are given. The use of MATLAB for solving problems involving parallel, series and cascaded two-port networks is shown. Example problems involving both passive and active circuits will be solved using MATLAB.

#### 7.1 TWO-PORT NETWORK REPRESENTATIONS

A general two-port network is shown in Figure 7.1.

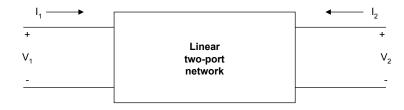


Figure 7.1 General Two-Port Network

 $I_1$  and  $V_1$  are input current and voltage, respectively. Also,  $I_2$  and  $V_2$  are output current and voltage, respectively. It is assumed that the linear two-port circuit contains no independent sources of energy and that the circuit is initially at rest (no stored energy). Furthermore, any controlled sources within the linear two-port circuit cannot depend on variables that are outside the circuit.

#### 7.1.1 z-parameters

A two-port network can be described by z-parameters as

$$V_1 = z_{11}I_1 + z_{12}I_2 \tag{7.1}$$

$$V_2 = z_{21}I_1 + z_{22}I_2 \tag{7.2}$$

In matrix form, the above equation can be rewritten as

$$\begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} z_{11} & z_{12} \\ z_{21} & z_{22} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$
(7.3)

The z-parameter can be found as follows

$$z_{11} = \frac{V_1}{I_1} \Big|_{I_2=0} \tag{7.4}$$

$$z_{12} = \frac{V_1}{I_2} \Big|_{I_1 = 0} \tag{7.5}$$

$$z_{21} = \frac{V_2}{I_1} \Big|_{I_2=0} \tag{7.6}$$

$$z_{22} = \frac{V_2}{I_2} \Big|_{I_1=0} \tag{7.7}$$

The z-parameters are also called open-circuit impedance parameters since they are obtained as a ratio of voltage and current and the parameters are obtained by open-circuiting port 2 ( $I_2 = 0$ ) or port1 ( $I_1 = 0$ ). The following example shows a technique for finding the z-parameters of a simple circuit.

### Example 7.1

For the T-network shown in Figure 7.2, find the z-parameters.

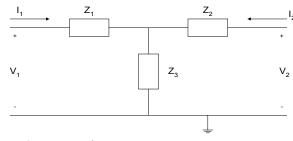


Figure 7.2 T-Network

## Solution

Using KVL

$$V_1 = Z_1 I_1 + Z_3 (I_1 + I_2) = (Z_1 + Z_3) I_1 + Z_3 I_2$$
(7.8)

$$V_2 = Z_2 I_2 + Z_3 (I_1 + I_2) = (Z_3) I_1 + (Z_2 + Z_3) I_2$$
(7.9)

thus

$$\begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} Z_1 + Z_3 & Z_3 \\ Z_3 & Z_2 + Z_3 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$
(7.10)

and the z-parameters are

$$[Z] = \begin{bmatrix} Z_1 + Z_3 & Z_3 \\ Z_3 & Z_2 + Z_3 \end{bmatrix}$$
(7.11)

## 7.1.2 y-parameters

A two-port network can also be represented using y-parameters. The describing equations are

$$I_1 = y_{11}V_1 + y_{12}V_2 \tag{7.12}$$

$$I_2 = y_{21}V_1 + y_{22}V_2 \tag{7.13}$$

where

 $V_1$  and  $V_2$  are independent variables and  $I_1$  and  $I_2$  are dependent variables.

In matrix form, the above equations can be rewritten as

$$\begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} y_{11} & y_{12} \\ y_{21} & y_{22} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix}$$
(7.14)

The y-parameters can be found as follows:

$$y_{11} = \frac{I_1}{V_1} \Big|_{V_2 = 0} \tag{7.15}$$

$$y_{12} = \frac{I_1}{V_2} \Big|_{V_1 = 0} \tag{7.16}$$

$$y_{21} = \frac{I_2}{V_1} \Big|_{V_2 = 0} \tag{7.17}$$

$$y_{22} = \frac{I_2}{V_2} \Big|_{V_1 = 0} \tag{7.18}$$

The y-parameters are also called short-circuit admittance parameters. They are obtained as a ratio of current and voltage and the parameters are found by short-circuiting port 2 ( $V_2 = 0$ ) or port 1 ( $V_1 = 0$ ). The following two examples show how to obtain the y-parameters of simple circuits.

## Example 7.2

Find the y-parameters of the pi ( $\pi$ ) network shown in Figure 7.3.

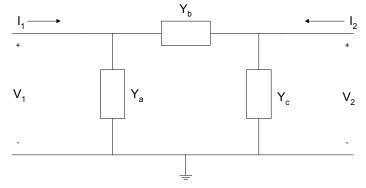


Figure 7.3 Pi-Network

#### Solution

Using KCL, we have

$$I_1 = V_1 Y_a + (V_1 - V_2) Y_b = V_1 (Y_a + Y_b) - V_2 Y_b$$
(7.19)

$$I_{2} = V_{2}Y_{c} + (V_{2} - V_{1})Y_{b} = -V_{1}Y_{b} + V_{2}(Y_{b} + Y_{c})$$
(7.20)

Comparing Equations (7.19) and (7.20) to Equations (7.12) and (7.13), the y-parameters are

$$[Y] = \begin{bmatrix} Y_a + Y_b & -Y_b \\ -Y_b & Y_b + Y_c \end{bmatrix}$$
(7.21)

# Example 7.3

Figure 7.4 shows the simplified model of a field effect transistor. Find its y-parameters.

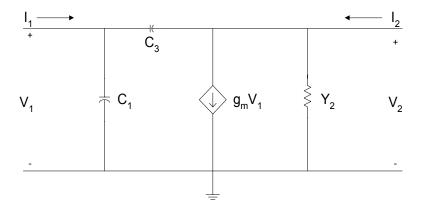


Figure 7.4 Simplified Model of a Field Effect Transistor

Using KCL,

$$I_{1} = V_{1}sC_{1} + (V_{1} - V_{2})sC_{3} = V_{1}(sC_{1} + sC_{3}) + V_{2}(-sC_{3})$$
(7.22)  
$$I_{2} = V_{2}Y_{2} + g_{m}V_{1} + (V_{2} - V_{1})sC_{3} = V_{1}(g_{m} - sC_{3}) + V_{2}(Y_{2} + sC_{3})$$
(7.23)

Comparing the above two equations to Equations (7.12) and (7.13), the y-parameters are

$$[Y] = \begin{bmatrix} sC_1 + sC_3 & -sC_3 \\ g_m - sC_3 & Y_2 + sC_3 \end{bmatrix}$$
(7.24)

## 7.1.3 h-parameters

A two-port network can be represented using the h-parameters. The describing equations for the h-parameters are

$$V_1 = h_{11}I_1 + h_{12}V_2 \tag{7.25}$$

$$I_2 = h_{21}I_1 + h_{22}V_2 \tag{7.26}$$

where

 $I_1$  and  $V_2$  are independent variables and  $V_1$  and  $I_2$  are dependent variables.

In matrix form, the above two equations become

$$\begin{bmatrix} V_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} \\ h_{21} & h_{22} \end{bmatrix} \begin{bmatrix} I_1 \\ V_2 \end{bmatrix}$$
(7.27)

The h-parameters can be found as follows:

$$h_{11} = \frac{V_1}{I_1} \Big|_{V_2 = 0} \tag{7.28}$$

$$h_{12} = \frac{V_1}{V_2} \Big|_{I_1 = 0} \tag{7.29}$$

$$h_{21} = \frac{I_2}{I_1} \Big|_{V_2 = 0} \tag{7.30}$$

$$h_{22} = \frac{I_2}{V_2} \Big|_{I_1 = 0} \tag{7.31}$$

The h-parameters are also called hybrid parameters since they contain both open-circuit parameters ( $I_1 = 0$ ) and short-circuit parameters ( $V_2 = 0$ ). The h-parameters of a bipolar junction transistor are determined in the following example.

# Example 7.4

A simplified equivalent circuit of a bipolar junction transistor is shown in Figure 7.5, find its h-parameters.

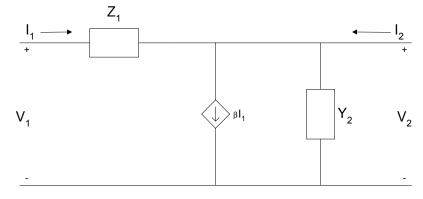


Figure 7.5 Simplified Equivalent Circuit of a Bipolar Junction Transistor

#### Solution

Using KCL for port 1,

$$V_1 = I_1 Z_1 \tag{7.32}$$

Using KCL at port 2, we get

$$I_2 = \beta I_1 + Y_2 V_2 \tag{7.33}$$

Comparing the above two equations to Equations (7.25) and (7.26) we get the h-parameters.

$$\begin{bmatrix} h \end{bmatrix} = \begin{bmatrix} Z_1 & 0\\ \beta & Y_2 \end{bmatrix}$$
(7.34)

#### 7.1.4 Transmission parameters

A two-port network can be described by transmission parameters. The describing equations are

$$V_1 = a_{11}V_2 - a_{12}I_2 \tag{7.35}$$

$$I_1 = a_{21}V_2 - a_{22}I_2 \tag{7.36}$$

where

 $V_2$  and  $I_2$  are independent variables and  $V_1$  and  $I_1$  are dependent variables.

In matrix form, the above two equations can be rewritten as

$$\begin{bmatrix} V_1 \\ I_1 \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} \begin{bmatrix} V_2 \\ -I_2 \end{bmatrix}$$
(7.37)

The transmission parameters can be found as

$$a_{11} = \frac{V_1}{V_2} \Big|_{I_2 = 0} \tag{7.38}$$

$$a_{12} = -\frac{V_1}{I_2}\Big|_{V_2=0}$$
(7.39)

$$a_{21} = \frac{I_1}{V_2} \Big|_{I_2 = 0} \tag{7.40}$$

$$a_{22} = -\frac{I_1}{I_2}\Big|_{V_2=0} \tag{7.41}$$

The transmission parameters express the primary (sending end) variables  $V_1$  and  $I_1$  in terms of the secondary (receiving end) variables  $V_2$  and  $-I_2$ . The negative of  $I_2$  is used to allow the current to enter the load at the receiving end. Examples 7.5 and 7.6 show some techniques for obtaining the transmission parameters of impedance and admittance networks.

# Example 7.5

Find the transmission parameters of Figure 7.6.

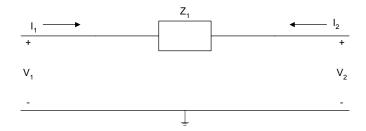


Figure 7.6 Simple Impedance Network

## Solution

By inspection,

$$I_1 = -I_2$$
 (7.42)

Using KVL,

$$V_1 = V_2 + Z_1 I_1 \tag{7.43}$$

Since  $I_1 = -I_2$ , Equation (7.43) becomes

$$V_1 = V_2 - Z_1 I_2 \tag{7.44}$$

Comparing Equations (7.42) and (7.44) to Equations (7.35) and (7.36), we have

$$a_{11} = 1 \qquad a_{12} = Z_1 a_{21} = 0 \qquad a_{22} = 1$$
(7.45)

## Example 7.6

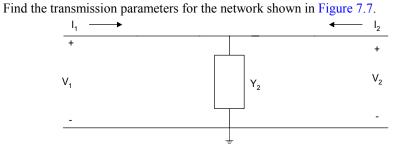


Figure 7.7 Simple Admittance Network

#### Solution

By inspection,

$$V_1 = V_2$$
 (7.46)

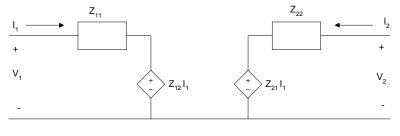
Using KCL, we have

$$I_1 = V_2 Y_2 - I_2 \tag{7.47}$$

Comparing Equations (7.46) and 7.47) to equations (7.35) and (7.36) we have

$$a_{11} = 1$$
  $a_{12} = 0$   
 $a_{21} = Y_2$   $a_{22} = 1$  (7.48)

Using the describing equations, the equivalent circuits of the various two-port network representations can be drawn. These are shown in Figure 7.8.



(a)

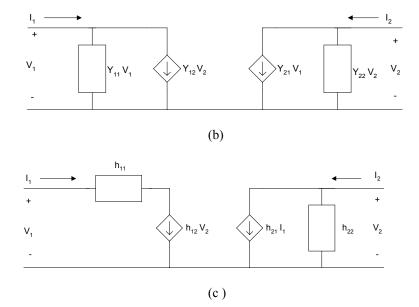
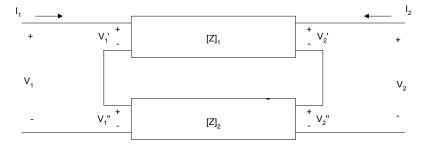


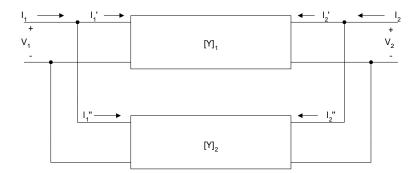
Figure 7.8 Equivalent Circuit of Two-port Networks (a) zparameters, (b) y-parameters and (c) h-parameters

# 7.2 INTERCONNECTION OF TWO-PORT NETWORKS

Two-port networks can be connected in series, parallel or cascade. Figure 7.9 shows the various two-port interconnections.



(a) Series-connected Two-port Network



(b) Parallel-connected Two-port Network

$I_1 \longrightarrow$	[	l <sup>I</sup> x →		$I_2 \longrightarrow$
+		+		+
V <sub>1</sub>	[A] <sub>1</sub>	V <sub>x</sub>	[A] <sub>2</sub>	V <sub>2</sub>

(c) Cascade Connection of Two-port Network

Figure 7.9 Interconnection of Two-port Networks (a) Series (b) Parallel (c) Cascade

It can be shown that if two-port networks with z-parameters  $[Z]_1, [Z]_2, [Z]_3, ..., [Z]_n$  are connected in series, then the equivalent two-port z-parameters are given as

$$[Z]_{eq} = [Z]_1 + [Z]_2 + [Z]_3 + \dots + [Z]_n$$
(7.49)

If two-port networks with y-parameters  $[Y]_1, [Y]_2, [Y]_3, ..., [Y]_n$  are connected in parallel, then the equivalent two-port y-parameters are given as

$$[Y]_{eq} = [Y]_1 + [Y]_2 + [Y]_3 + \dots + [Y]_n$$
(7.50)

When several two-port networks are connected in cascade, and the individual networks have transmission parameters  $[A]_1, [A]_2, [A]_3, ..., [A]_n$ , then the equivalent two-port parameter will have a transmission parameter given as

$$[A]_{eq} = [A]_1 * [A]_2 * [A]_3 * \dots * [A]_n$$
(7.51)

The following three examples illustrate the use of MATLAB for determining the equivalent parameters of interconnected two-port networks.

# Example 7.7

Find the equivalent y-parameters for the bridge T-network shown in Figure 7.10.

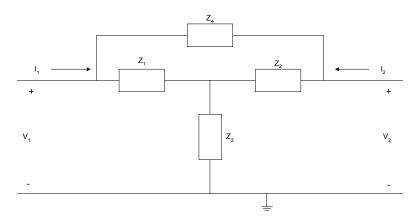


Figure 7.10 Bridge-T Network

## Solution

The bridge-T network can be redrawn as

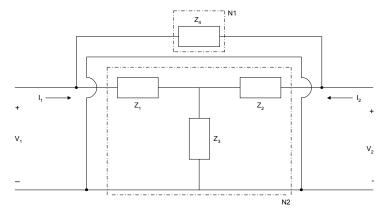


Figure 7.11 An Alternative Representation of Bridge-T Network

From Example 7.1, the z-parameters of network N2 are

$$[Z] = \begin{bmatrix} Z_1 + Z_3 & Z_3 \\ Z_3 & Z_2 + Z_3 \end{bmatrix}$$

We can convert the z-parameters to y-parameters [refs. 4 and 6] and we get

$$y_{11} = \frac{Z_2 + Z_3}{Z_1 Z_2 + Z_1 Z_3 + Z_2 Z_3}$$

$$y_{12} = \frac{-Z_3}{Z_1 Z_2 + Z_1 Z_3 + Z_2 Z_3}$$

$$y_{21} = \frac{-Z_3}{Z_1 Z_2 + Z_1 Z_3 + Z_2 Z_3}$$

$$y_{22} = -\frac{Z_1 + Z_3}{Z_1 Z_2 + Z_1 Z_3 + Z_2 Z_3}$$
(7.52)

From Example 7.5, the transmission parameters of network N1 are

$$a_{11} = 1$$
  $a_{12} = Z_4$   
 $a_{21} = 0$   $a_{22} = 1$ 

We convert the transmission parameters to y-parameters[ refs. 4 and 6] and we get

$$y_{11} = \frac{1}{Z_4}$$

$$y_{12} = -\frac{1}{Z_4}$$

$$y_{21} = -\frac{1}{Z_4}$$

$$y_{22} = \frac{1}{Z_4}$$
(7.53)

Using Equation (7.50), the equivalent y-parameters of the bridge-T network are

$$y_{11eq} = \frac{1}{Z_4} + \frac{Z_2 + Z_3}{Z_1 Z_2 + Z_1 Z_3 + Z_2 Z_3}$$

$$y_{12eq} = -\frac{1}{Z_4} - \frac{Z_3}{Z_1 Z_2 + Z_1 Z_3 + Z_2 Z_3}$$

$$y_{21eq} = -\frac{1}{Z_4} - \frac{Z_3}{Z_1 Z_2 + Z_1 Z_3 + Z_2 Z_3}$$

$$y_{22eq} = \frac{1}{Z_4} + \frac{Z_1 + Z_3}{Z_1 Z_2 + Z_1 Z_3 + Z_2 Z_3}$$
(7.54)

# Example 7.8

Find the transmission parameters of Figure 7.12.

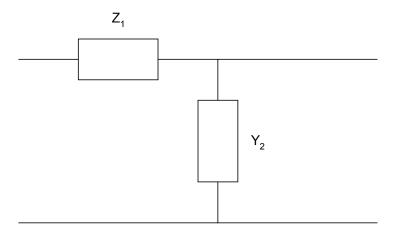


Figure 7.12 Simple Cascaded Network

# Solution



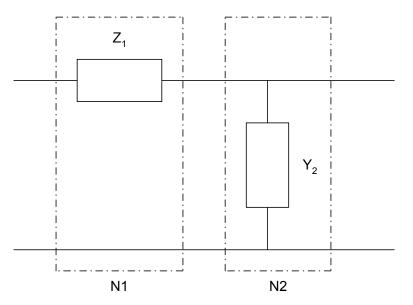


Figure 7.13 Cascade of Two Networks N1 and N2

From Example 7.5, the transmission parameters of network N1 are

$$a_{11} = 1$$
  $a_{12} = Z_1$   
 $a_{21} = 0$   $a_{22} = 1$ 

From Example 7.6, the transmission parameters of network N2 are

$$a_{11} = 1$$
  $a_{12} = 0$   
 $a_{21} = Y_2$   $a_{22} = 1$ 

From Equation (7.51), the transmission parameters of Figure 7.13 are

$$\begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}_{eq} = \begin{bmatrix} 1 & Z_1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ Y_2 & 1 \end{bmatrix} = \begin{bmatrix} 1 + Z_1 Y_2 & Z_1 \\ Y_2 & 1 \end{bmatrix}$$
(7.55)

## Example 7.9

Find the transmission parameters for the cascaded system shown in Figure 7.14. The resistance values are in Ohms.

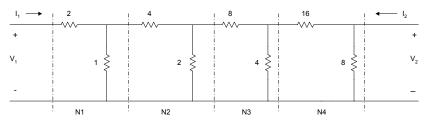


Figure 7.14 Cascaded Resistive Network

#### Solution

Figure 7.14 can be considered as four networks, N1, N2, N3, and N4 connected in cascade. From Example 7.8, the transmission parameters of Figure 7.12 are

$$[a]_{N1} = \begin{bmatrix} 3 & 2 \\ 1 & 1 \end{bmatrix}$$
$$[a]_{N2} = \begin{bmatrix} 3 & 4 \\ 0.5 & 1 \end{bmatrix}$$
$$[a]_{N3} = \begin{bmatrix} 3 & 8 \\ 0.25 & 1 \end{bmatrix}$$
$$[a]_{N4} = \begin{bmatrix} 3 & 16 \\ 0.125 & 1 \end{bmatrix}$$

The transmission parameters of Figure 7.14 can be obtained using the following MATLAB program.

#### MATLAB Script

diary ex7\_9.dat % Transmission parameters of cascaded network

a1 = [3 2; 1 1]; a2 = [3 4; 0.5 1]; a3 = [3 8; 0.25 1];a4 = [3 16; 0.125 1];

% equivalent transmission parameters a = a1\*(a2\*(a3\*a4)) diary

The value of matrix a is

a = 112.2500 630.0000 39.3750 221.0000

#### 7.3 TERMINATED TWO-PORT NETWORKS

In normal applications, two-port networks are usually terminated. A terminated two-port network is shown in Figure 7.4.

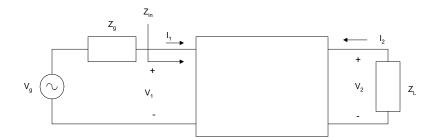


Figure 7.15 Terminated Two-Port Network

In the Figure 7.15,  $V_g$  and  $Z_g$  are the source generator voltage and impedance, respectively.  $Z_L$  is the load impedance. If we use z-parameter representation for the two-port network, the voltage transfer function can be shown to be

$$\frac{V_2}{V_g} = \frac{z_{21}Z_L}{(z_{11} + Z_g)(z_{22} + Z_L) - z_{12}z_{21}}$$
(7.56)

and the input impedance,

$$Z_{in} = z_{11} - \frac{z_{12} z_{21}}{z_{22} + Z_L}$$
(7.57)

and the current transfer function,

$$\frac{I_2}{I_1} = -\frac{z_{21}}{z_{22} + Z_L} \tag{7.58}$$

A terminated two-port network, represented using the y-parameters, is shown in Figure 7.16.

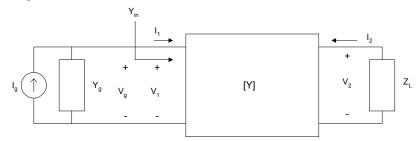


Figure 7.16 A Terminated Two-Port Network with y-parameters Representation

It can be shown that the input admittance,  $Y_{in}$ , is

$$Y_{in} = y_{11} - \frac{y_{12}y_{21}}{y_{22} + Y_L}$$
(7.59)

and the current transfer function is given as

$$\frac{I_2}{I_g} = \frac{y_{21}Y_L}{(y_{11} + Y_g)(y_{22} + Y_L) - y_{12}y_{21}}$$
(7.60)

and the voltage transfer function

$$\frac{V_2}{V_g} = -\frac{y_{21}}{y_{22} + Y_L} \tag{7.61}$$

A doubly terminated two-port network, represented by transmission parameters, is shown in Figure 7.17.

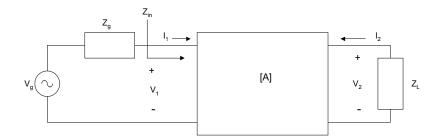


Figure 7.17 A Terminated Two-Port Network with Transmission Parameters Representation

The voltage transfer function and the input impedance of the transmission parameters can be obtained as follows. From the transmission parameters, we have

$$V_1 = a_{11}V_2 - a_{12}I_2 \tag{7.62}$$

$$I_1 = a_{21}V_2 - a_{22}I_2 \tag{7.63}$$

From Figure 7.6,

$$V_2 = -I_2 Z_L (7.64)$$

Substituting Equation (7.64) into Equations (7.62) and (7.63), we get the input impedance,

$$Z_{in} = \frac{a_{11}Z_L + a_{12}}{a_{21}Z_L + a_{22}}$$
(7.65)

From Figure 7.17, we have

$$V_1 = V_g - I_1 Z_g (7.66)$$

Substituting Equations (7.64) and (7.66) into Equations (7.62) and (7.63), we have

$$V_g - I_1 Z_g = V_2 [a_{11} + \frac{a_{12}}{Z_L}]$$
(7.67)

$$I_1 = V_2 \left[ a_{21} + \frac{a_{22}}{Z_L} \right] \tag{7.68}$$

Substituting Equation (7.68) into Equation (7.67), we get

$$V_g - V_2 Z_g [a_{21} + \frac{a_{22}}{Z_L}] = V_2 [a_{11} + \frac{a_{12}}{Z_L}]$$
(7.69)

Simplifying Equation (7.69), we get the voltage transfer function

$$\frac{V_2}{V_g} = \frac{Z_L}{(a_{11} + a_{21}Z_g)Z_L + a_{12} + a_{22}Z_g}$$
(7.70)

The following examples illustrate the use of MATLAB for solving terminated two-port network problems.

#### Example 7.10

Assuming that the operational amplifier of Figure 7.18 is ideal,

- (a) Find the z-parameters of Figure 7.18.
- (b) If the network is connected by a voltage source with source resistance of  $50\Omega$  and a load resistance of  $1 \text{ K}\Omega$ , find the voltage gain.
- (c) Use MATLAB to plot the magnitude response.

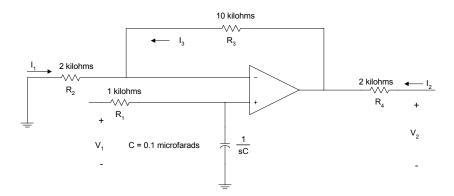


Figure 7.18 An Active Lowpass Filter

#### Solution

Using KVL,

$$V_1 = R_1 I_1 + \frac{I_1}{sC}$$
(7.71)

$$V_2 = R_4 I_2 + R_3 I_3 + R_2 I_3 \tag{7.72}$$

From the concept of virtual circuit discussed in Chapter 11,

$$R_2 I_3 = \frac{I_1}{sC}$$
(7.73)

Substituting Equation (7.73) into Equation (7.72), we get

$$V_2 = \frac{\left(R_2 + R_3\right)I_1}{sCR_2} + R_4I_2 \tag{7.74}$$

Comparing Equations (7.71) and (7.74) to Equations (7.1) and (7.2), we have

$$z_{11} = R_1 + \frac{1}{sC}$$

$$z_{12} = 0$$

$$z_{21} = \left(1 + \frac{R_3}{R_2}\right) \left(\frac{1}{sC}\right)$$

$$z_{22} = R_4$$
(7.75)

From Equation (7.56), we get the voltage gain for a terminated two-port network. It is repeated here.

$$\frac{V_2}{V_g} = \frac{z_{21}Z_L}{(z_{11} + Z_g)(z_{22} + Z_L) - z_{12}z_{21}}$$

Substituting Equation (7.75) into Equation (7.56), we have

$$\frac{V_2}{V_g} = \frac{(1 + \frac{R_3}{R_2})Z_L}{(R_4 + Z_L)[1 + sC(R_1 + Z_g)]}$$
(7.76)

For  $Z_g = 50 \Omega$ ,  $Z_L = 1 K\Omega$ ,  $R_3 = 10 K\Omega$ ,  $R_2 = 1 K\Omega$ ,  $R_4 = 2 K\Omega$ and  $C = 0.1 \mu F$ , Equation (7.76) becomes

$$\frac{V_2}{V_g} = \frac{2}{[1+1.05*10^{-4}s]}$$
(7.77)

The MATLAB script is

% num = [2]; den = [1.05e-4 1]; w = logspace(1,5); h = freqs(num,den,w); f = w/(2\*pi); mag = 20\*log10(abs(h)); % magnitude in dB semilogx(f,mag) title('Lowpass Filter Response') xlabel('Frequency, Hz') ylabel('Gain in dB')

The frequency response is shown in Figure 7.19.

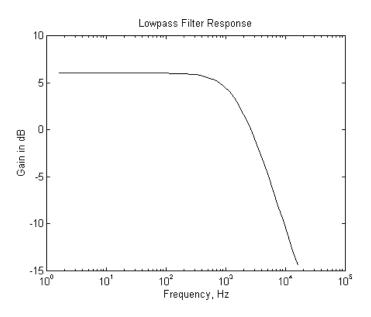


Figure 7.19 Magnitude Response of an Active Lowpass Filter

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## EXERCISES

7.1 (a) Find the transmission parameters of the circuit shown in Figure P7.1a. The resistance values are in ohms.

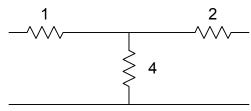


Figure P7.1a Resistive T-Network

(b) From the result of part (a), use MATLAB to find the transmission parameters of Figure P7.2b. The resistance values are in ohms.

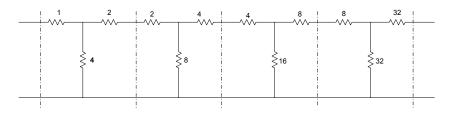


Figure P7.1b Cascaded Resistive Network

**7.2** Find the y-parameters of the circuit shown in Figure P7.2 The resistance values are in ohms.

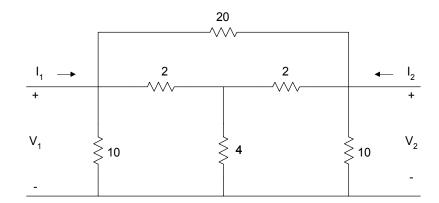


Figure P7.2 A Resistive Network

**7.3** (a) Show that for the symmetrical lattice structure shown in Figure P7.3,

$$z_{11} = z_{22} = 0.5(Z_c + Z_d)$$
$$z_{12} = z_{21} = 0.5(Z_c - Z_d)$$

(b) If  $Z_c = 10 \Omega$ ,  $Z_d = 4 \Omega$ , find the equivalent yparameters.

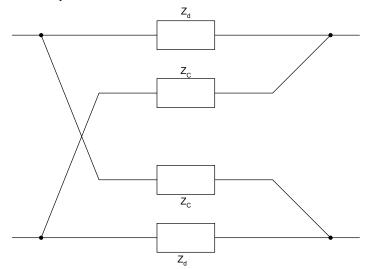


Figure P7.3 Symmetrical Lattice Structure

7.4 (a) Find the equivalent z-parameters of Figure P7.4. (b) If the network is terminated by a load of 20 ohms and connected to a source of  $V_s$  with a source resistance of 4 ohms, use MATLAB to plot the frequency response of the circuit.

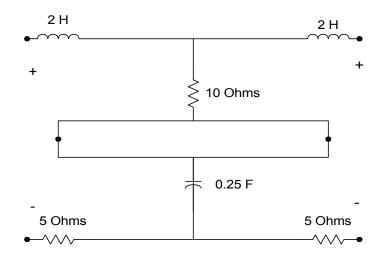


Figure P7.4 Circuit for Problem 7.4

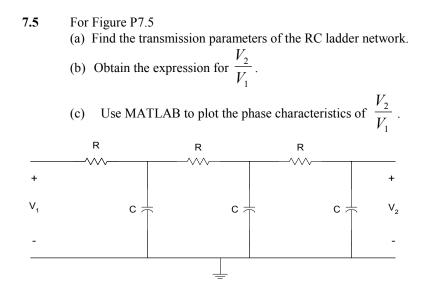


Figure P7.5 RC Ladder Network

**7.6** For the circuit shown in Figure P7.6,

- (a) Find the y-parameters.
- (b) Find the expression for the input admittance.
- (c) Use MATLAB to plot the input admittance as a function of frequency.

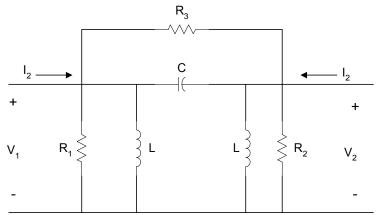


Figure P7.6 Circuit for Problem 7.6

7.7 For the op amp circuit shown in Figure P7.7, find the y-parameters.

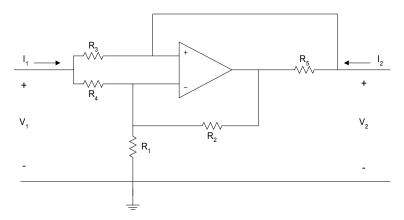


Figure P7.7 Op Amp Circuit