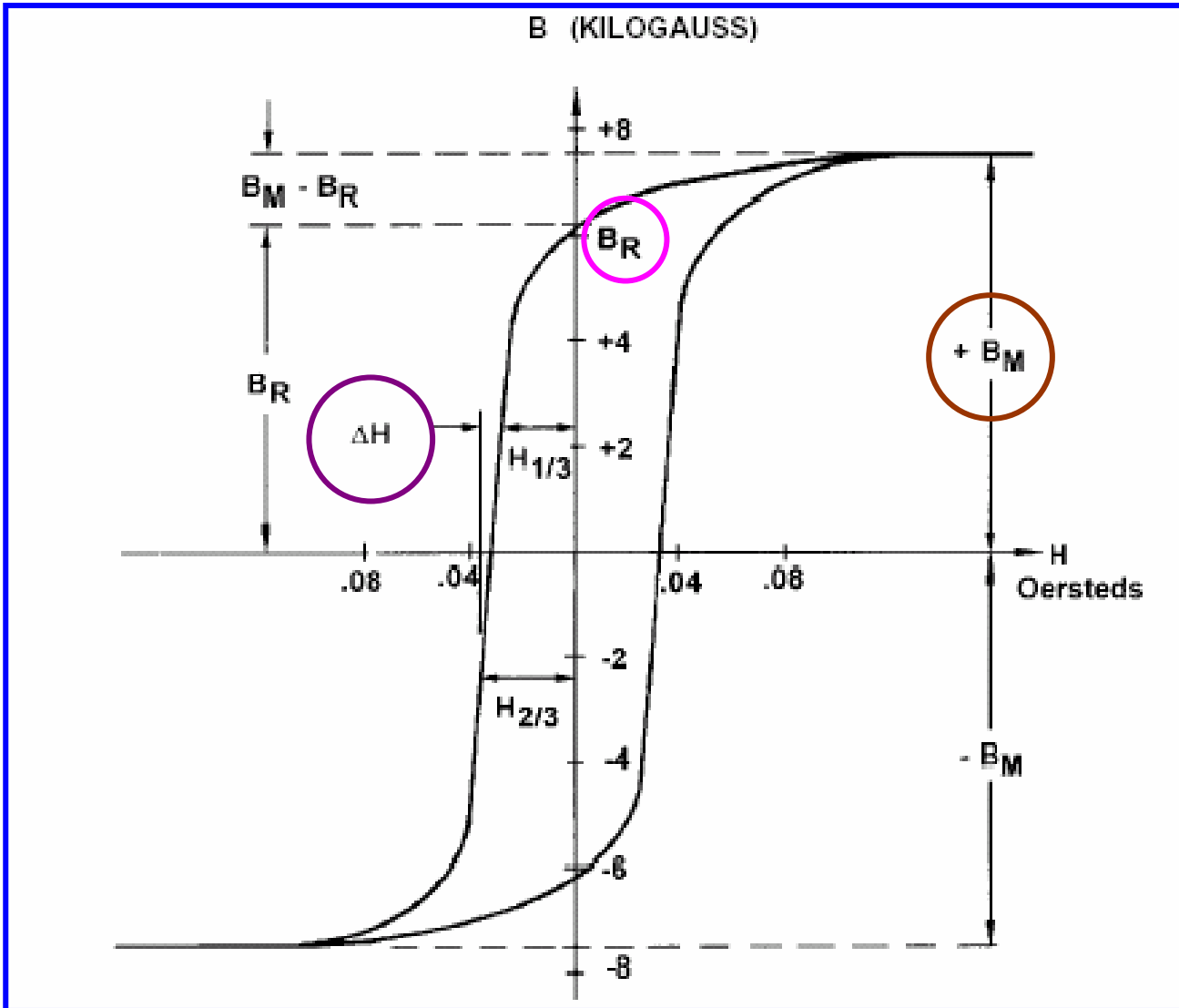


# Technical Training

Adlsong

# Basic Theory



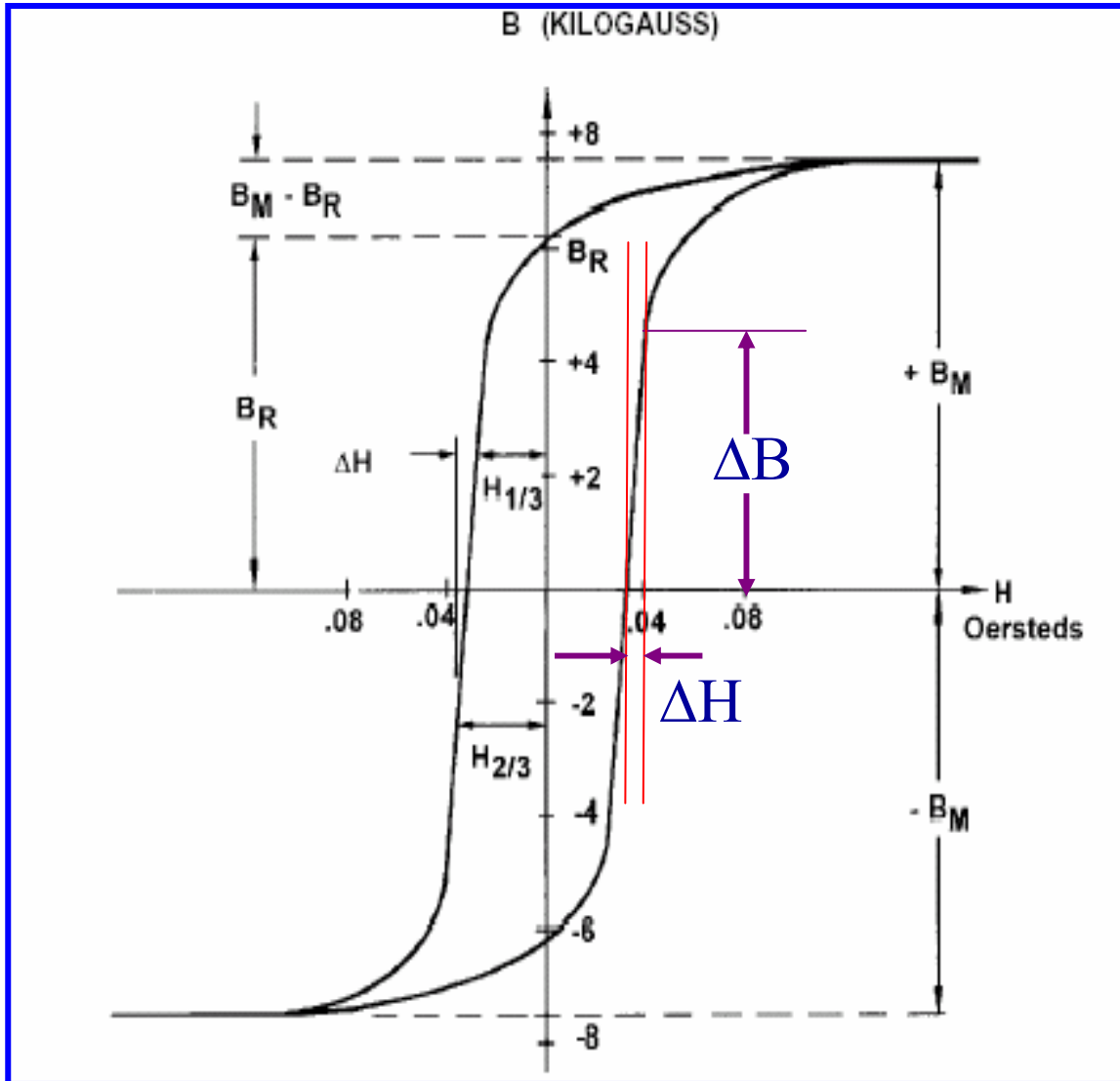
## Hysteresis Loop

**$B_s$** : saturate magnetic flux density

**$B_r$** : residual magnetic flux density

**$H_c$** : coercive force

# Basic Theory



## Hysteresis Loop

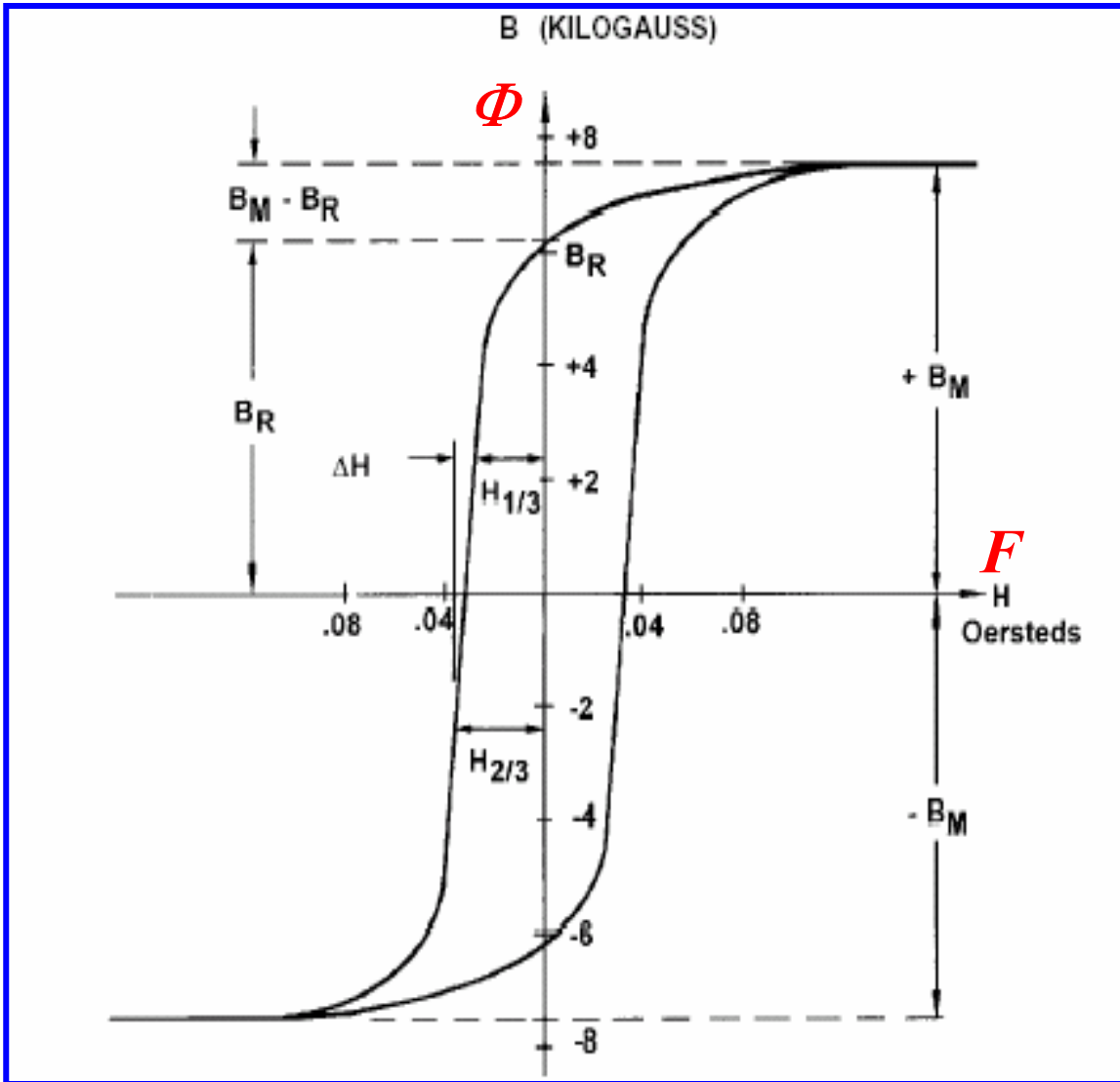
$$B = \mu \cdot H$$

**B**: flux density (tesla)

**H**: field intensity (A-T/m)

**μ**: permeability

# Basic Theory



## Hysteresis Loop

$X$                        $Y$

$H$                        $B$

$F$  ( $F = H \cdot l$ )       $\Phi$  ( $\Phi = B \cdot A$ )

$A$ : core effective area ( $m^2$ )

$\Phi$ : flux ( $T \cdot m^2$  or webers)

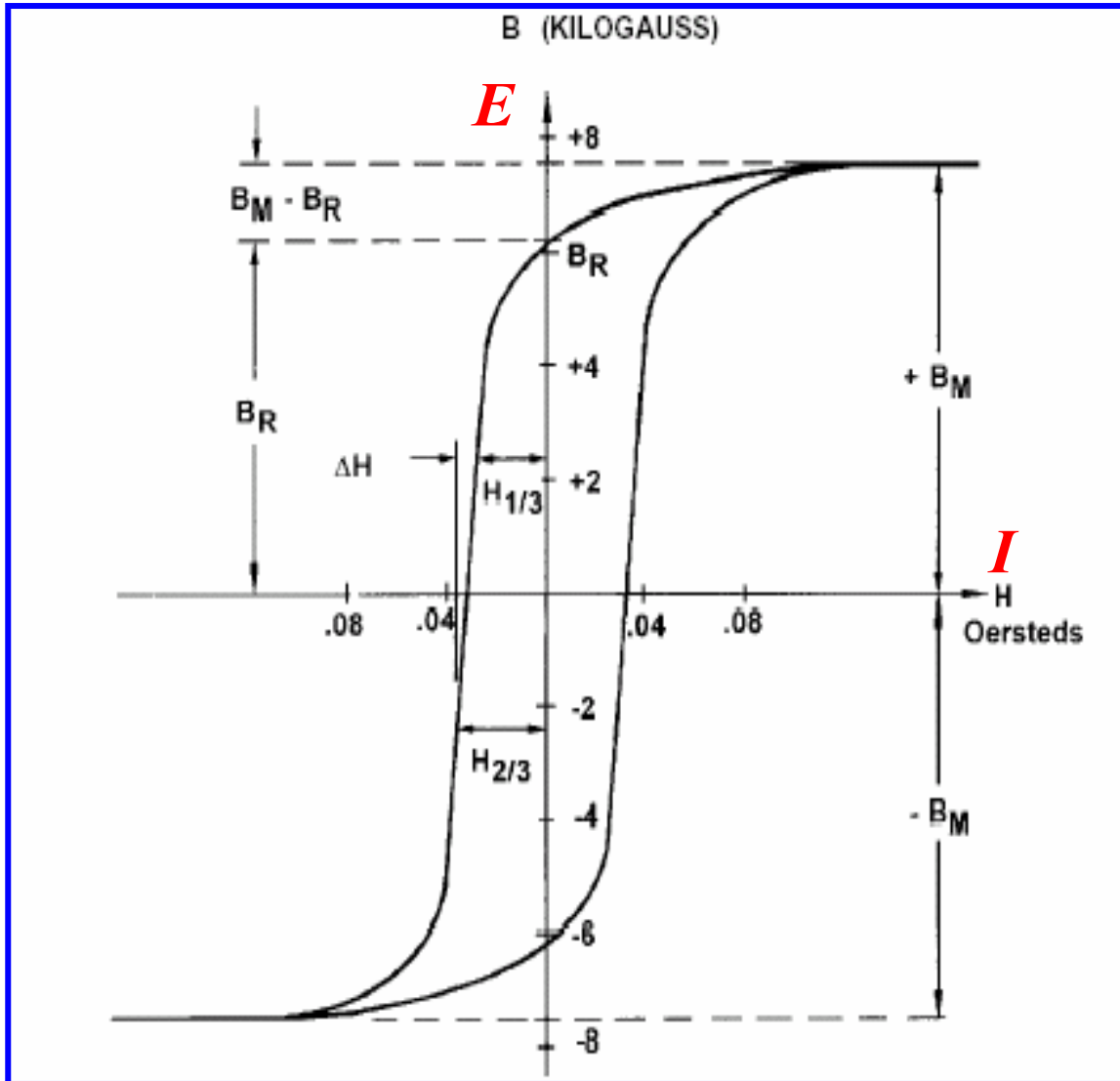
$F$ : magnetic force (ampere-turns)

$l$ : path length (m)

$B - H$ : defining a core material

$\Phi - F$ : defining a specific core  
with  $A_e$  and  $l_e$

# Basic Theory



## Hysteresis Loop

X Y

H B

$I (I=H/N)$   $E (E=Nd\Phi/dt)$

$E - I$ : defining a specific core wound with N turns

# Basic Theory

## Two Important Laws

① **Ampere's Law:**  $F = \int H \cdot dl = \Sigma H \cdot l = N \cdot I$

I : loop current (ampere)

N : turns of windings

② **Faraday's Law:**  $E = N d\Phi / dt$

E: induced voltage (volts)

Flux cannot change instantaneously:

The time is required to move along B( $\Phi$ ) and a change in energy takes place

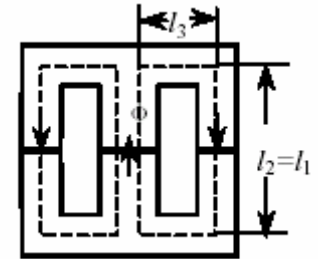
# Basic Theory

## Without air gap:

$$W = \int Vol \cdot HdB = \int I \cdot Edt \quad (W/m^3 = 0.5 \cdot H \cdot B)$$

$$L = N \cdot \Phi / i = \mu_0 \cdot N^2 \cdot A / l = A_L \cdot N^2$$

$A_L$ : inductance factor



## With air gap:

$$W = \int Vol \cdot HdB = V \cdot B^2 / 2\mu + Vg \cdot B^2 / 2\mu_0$$

$$L = \mu_0 N^2 A / (l/\mu_r + g) \approx \mu_0 N^2 A / g = A_L \cdot N^2$$

$$B = \mu_0 NI / (g + l/\mu_r)$$

Note: Most of the energy is stored in the gap portion

$$\mu \gg \mu_0, \quad 1/\mu_r \gg g$$

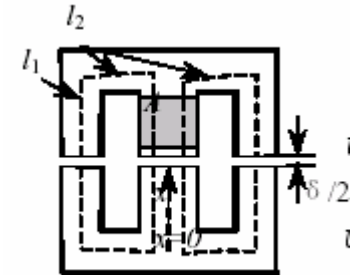
$g$ : air gap length

$l$ : magnetic path length

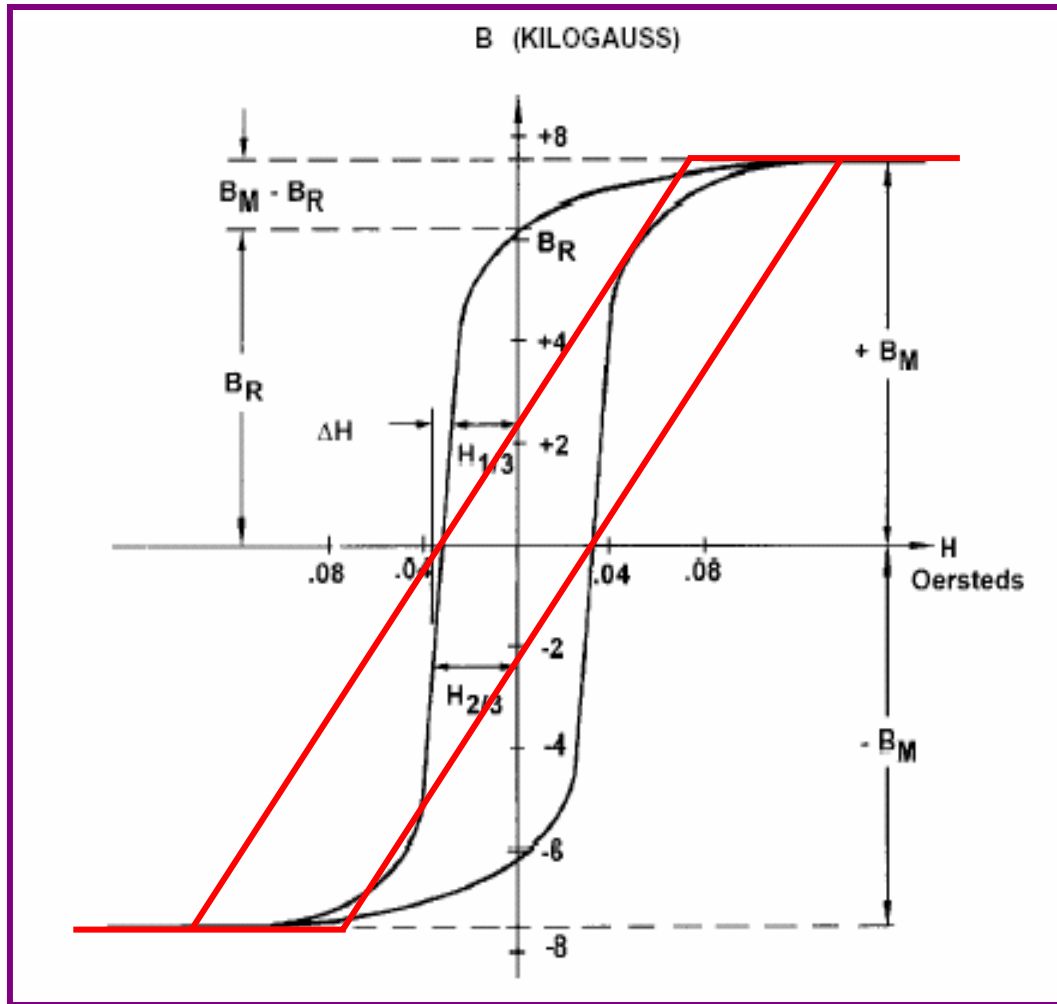
$\mu$ : magnetic core permeability

$\mu_0$ : space permeability

$\mu_r$ : relative permeability



# Basic Theory



As for the same current:

Effective flux density of no air gap magnetic core is decreased compared with air gap magnetic core

**Low value section of hysteresis loop is**  
Very linearized



# Basic Theory

## 2.1 Three types of devices

Resistor:  $u/i = R$

$u, i$  can change instantaneously

Inductor:  $L \cdot di_L/dt = u_L$

$i$  cannot change instantaneously

Capacitor:  $C \cdot du_C/dt = i_C$

$u$  cannot change instantaneously

# Basic Theory

## 2.2 ZCT

$$L \cdot di_L/dt = u_C$$

$$i_L = -i_C = -C \cdot du_C/dt$$

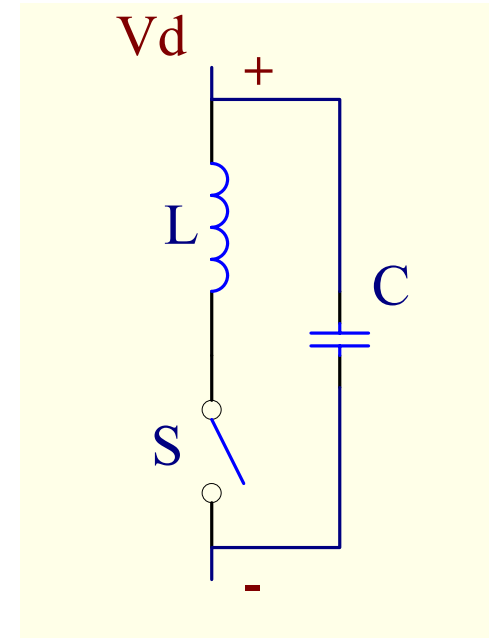
$$i_{C(0)} = 0, i_{L(0)} = 0, U_{C(0)} = U_d$$

$$\text{So: } u_C = U_d \cdot \cos \omega t$$

$$i_L = U_d \cdot \sin \omega t / Z_c$$

$$\omega_0 = (1/LC)^{1/2}$$

$$Z_c = (L/C)^{1/2}$$



# Basic Theory

- (1) Resonant tanks: LC, L and S in series, S is off at the beginning. The resonant process is starting when S is switched on.
- (2)  $\omega_0 t = k\pi$ ,  $i_L = 0$ , ZCT when  $i_L = 0$ .
- (3) half wave : the current cannot be reverse after  $\omega_0 t = k\pi$  because S is off
- (4) Full wave when a diode is in parallel with S –current: forward and reverse direction).

# Basic Theory

## 2.3 ZVT

$$L \cdot di_L/dt + u_C = U_d$$

$$i_L = i_C = C \cdot du_C/dt$$

$$i_{C(0)} = 0, u_{C(0)} = 0, U_{C(0)} = U_d$$

$$C \cdot du_C/dt = I_{L0}$$

So:

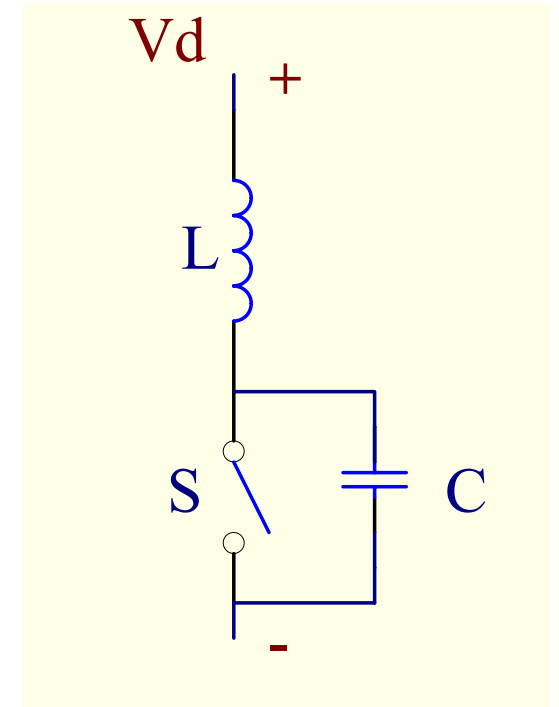
$$u_C = U_d \cdot (1 + (1 + (Z_0 I_{L0} / U_d)^2)^{1/2}) \sin(\omega_0 t - a)$$

$$i_L = U_d \cdot \sin \omega_0 t / Z_c$$

$$\omega_0 = (1/LC)^{1/2}$$

$$Z_0 = (L/C)^{1/2}$$

$$a = \arctg U_d / Z_0 I_{L0}$$



(1) Resonant tanks: LC, C and S in parallel, S is on at the beginning. The resonant process is starting when S is switched off.

(2)  $\omega_0 t - a = 0, u_C > 0; \omega_0 t - a = 3/2\pi, u_L < 0$ . ZVT when  $u_C = 0$ .

(3) full wave : the voltage can be reverse after  $u_C = 0$   
(4) half wave when a diode is in parallel with S

--the voltage is clamped by the diode.