Use of Leading-Edge Modulation to Transform Boost and Flyback Converters into Minimum-Phase-Zero Systems

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Abstract—It is shown how leading-edge modulation can shift the undesirable right-half-plane (positive) zero of boost and flyback converters into the left-half-plane. This allows a substantial improvement in the closed-loop characteristics by yielding a minimum phase system. Several techniques are employed to predict this result. The design procedure for shifting the positive zero into the left-half-plane is presented. Experimental verification is provided.

I. INTRODUCTION

A. Background

STATE-SPACE averaging [1] predicts a positive zero in the control-to-output transfer function of boost and flyback converters operating in the continuous mode. The 90 degree phase lag severely constrains the loop gain crossover to a frequency much lower than the right-half-plane zero. This limits the dynamic performance of the converter.

The PWM Switch Model [2] is an alternative average modelling technique that is easier to implement in circuit analysis programs such as SPICE. The small-signal characteristics of the PWM switch model are identical to state-space averaging in the continuous conduction mode. It is used throughout this paper.

Average models, however, do not accurately predict the behavior of power converters under all circumstances. It has been shown [3] that when the error compensation signal is pulsating due to the ESR of the output capacitance, then the Discrete-Average Model has better accuracy. The Discrete-Average Model employs the identical averaging of the state variables. The only difference is that the output equation is not averaged. The output equation of the converter power state depends on the type of modulation that is performed in the pulsewidth modulator. This is described later in detail.

Conventional PWM converters are designed with trailing-edge modulation. In trailing-edge modulation, the PWM signal is turned on at the clock signal and turned off when the error signal intersects the ramp waveform.

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Almost all commercially available PWM integrated circuits operate on this principle. However, it is just as easy to implement leading-edge modulation. In leading-edge modulation, the PWM signal is turned off at the clock signal and turned on when the error signal crosses the ramp waveform.

It is shown that the positive zero in the power stage transfer function of boost and flyback regulators can be shifted into the left-half-plane under suitable conditions. These conditions are as follows:

- 1) Leading-edge modulation must be employed in the pulse-width-modulator.
- 2) The feedback compensation must not average the ESR-generated output voltage switching ripple.
- 3) Appropriate power stage parameter values are necessary.

B. Motivation

The motivation behind this study originated after a stability analysis of a spacecraft battery discharger employing a boost topology could not predict the converters' excellent performance and stability. The converter, which was designed in the early 1970's, has been operating in space, flawlessly, for about 15 years. The stability analysis, however, which employed the state-space averaging technique, indicated that the converter should be unstable.

II. Modeling Techniques

A. Waveform Analysis

Systems that contain a right-half-plane zero, often referred to as nonminimum phase systems, have a characteristic step input response shown in Fig. 1. The output will initially drop prior to rising and reaching steady state.

In boost and buck-boost derived converters, an incremental step increase in duty cycle translates to increased capacitor hold-up time for the output voltage. This will cause the average output voltage to initially drop until the inductor current builds up to recharge the capacitor. The lag time from the initial drop until the voltage returns to the initial value is inversely proportional to the positive zero.

However, depending on the dynamics of the feedback

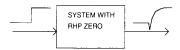


Fig. 1. Nonminimum-phase-zero characteristic step response. Step input response of system containing positive zero will initially decrease prior to rising and reaching steady state.

compensation network, the PWM error processor may respond to the instantaneous output voltage. When conventional trailing-edge modulation is employed, the PWM responds to the instantaneous voltage prior to the switch turning off. When leading-edge modulation is employed, the PWM responds to the instantaneous voltage prior to the switch turning on.

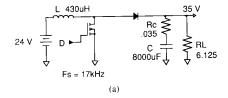
Fig. 2(a) shows a boost regulator schematic that was simulated in SPICE. Fig. 2(b) shows the switch current waveform. At t = 3 ms, a step increase in duty cycle occurs. The inductor current increases immediately (labeled point A on the figure). The control-to-inductor current transfer function does not contain a positive zero. Fig. 2(c) shows the voltage waveform directly across the output capacitor. At the step increase in duty cycle, the capacitor voltage waveform initially drops before recovering. This is true for the average capacitor voltage, as well as the instantaneous voltage after the switch turns off (labeled point B on the figure) and the instantaneous voltage after the switch turns on again (labeled point C on the figure). The positive zero cannot be shifted in the controlto-capacitor voltage transfer function. The capacitor voltage is the same as the average output voltage. Fig. 2(d) shows the output voltage waveform. At the instant that the switch turns off or on, there is a discontinuous jump in the output voltage due to the voltage drop across the capacitor ESR. At the step increase in duty cycle, the instantaneous output voltage, prior to switch turn-off, (labeled point D on the figure) initially drops, as in the capacitor voltage. Thus, when employing trailing-edge modulation, the positive zero cannot be shifted into the left-half-plane. The instantaneous output voltage prior to switch turn on, (labeled point E on the figure) however, increases.

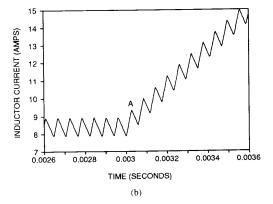
The condition whereby the instantaneous output voltage prior to switch turn on increases in response to an incremental increase in duty cycle can be approximately derived by viewing the steady state waveforms shown in Fig. 3. It is dependent on the steady state duty cycle, the power inductance, capacitance, load resistance, and capacitor ESR values.

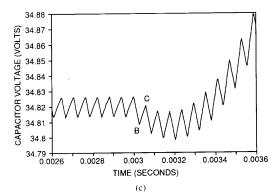
The output voltage, v_{o1} , at the instant prior to the switch turning on is the sum of the instantaneous capacitor and ESR voltages:

$$v_{o1} = v_{c1} + v_{rc1}. (1)$$

The instantaneous capacitor voltage prior to the switch turning on is equal to the average output voltage plus the change in capacitor voltage due to the average charging current.







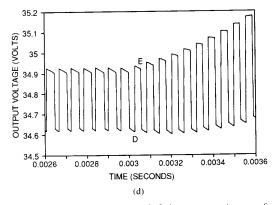


Fig. 2. (a) Simulated boost converter. (b) Inductor current time waveform. At step increase in duty cycle at t=3 ms, inductor current immediately rises indicating no positive zero in duty cycle to inductor current transfer function. (c) Capacitor voltage time waveform. At step increase in duty cycle, capacitor voltage waveform decreases prior to increasing. This indicates that duty cycle to capacitor voltage transfer function contains positive zero. (d) Output voltage time waveform. At step increase in duty cycle, valley of output voltage waveform (D) initially decreases prior to increasing. Peak of output voltage waveform (E) increases immediately.

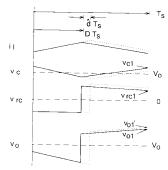


Fig. 3. Steady state waveforms.

$$v_{c1} = V_o \left(1 + \frac{dT_s}{2R_L C} \right). \tag{2}$$

The instantaneous ESR voltage prior to the switch turning on is given by

$$v_{rc1} = V_o \left(\frac{R_c}{R_L (1 - d)} - \frac{(1 - d) dT_s R_c}{2L} \right).$$
 (3)

Let $d = D + \hat{d}$. The new value of the output voltage at the instant prior to switch turning on, v'_{o1} , is derived in terms of the old value, v_{o1} , plus a function of the incremental duty cycle:

$$v'_{o1} = v_{o1} + \hat{d}T_s V_o \left(\frac{R_c}{L} - \frac{1}{R_L C(1-D)}\right).$$
 (4)

To shift the positive zero into the left-half-plane, the new value of the output voltage at the instant prior to the switch turning on must be greater that the old value. This condition is given by:

$$R_c C > \frac{L}{R_L D'} \tag{5}$$

B. Discrete-Average Model Mathematical Derivation

State-space averaging is implemented by writing the state equations and output equation for the linear networks corresponding the switch-on and switch-off conditions. The equations are then weighted according to the switch-on and switch-off periods:

$$\dot{x} = (dA_1 + d'A_2)x + (dB_1 + d'B_2)u \tag{6}$$

$$v_o = (dC_1 + d'C_2)x. (7)$$

These equations are then linearized in order to obtain the equivalent small signal circuit and the resulting transfer functions. The Discrete-Average Model is similar to the average model in that the average of the state variables is used. However, the output voltage is determined by discrete samples. The sample point is dependent on whether trailing-edge or leading-edge modulation is employed. When conventional trailing-edge modulation is employed, the PWM responds to the instantaneous output

voltage while the switch is on in order to determine the termination point of the on time:

$$v_{\alpha} = C_1 x. \tag{8}$$

When leading-edge modulation is employed, the PWM responds to the instantaneous output voltage while the switch is off in order to determine the termination point of the off time:

$$v_o = C_2 x. (9)$$

This leads to some subtle differences in the control-tooutput transfer function of the three models. The controlto-output transfer function of the Average model is given by

$$\frac{\hat{v}_o}{\hat{d}} = \frac{V_i}{D'^2} \frac{(1 + s/\omega_c)(1 - s/\omega_a)}{(1 + s/\omega_a Q + s^2/\omega_o^2)}$$
(10)

where

$$\omega_z = \frac{1}{R_c C}, \qquad \omega_a = \frac{D'^2 R_L}{L} \tag{11}$$

$$\omega_o = \frac{D'}{\sqrt{LC}}, \qquad Q = \frac{D'}{\omega_o} \frac{1}{\frac{L}{D'R_L} + R_cC}.$$
 (12)

The control-to-output transfer function of the Discrete-Average model for trailing-edge modulation is given by

$$\frac{\hat{v}_o}{\hat{d}} = \frac{V_i}{D^{'2}} \frac{(1 - s/\omega_a)}{(1 + s/\omega_a Q + s^2/\omega_o^2)}.$$
 (13)

The control-to-output transfer function of the Discrete-Average model for leading-edge modulation is given by

$$\frac{\hat{v}_o}{\hat{d}} = \frac{V_i}{D'^2} \frac{(1 + s/\omega_{a1})}{(1 + s/\omega_o Q + s^2/\omega_o^2)}$$
(14)

where

$$\omega_{a1} = \frac{1}{\frac{R_c C}{D'} - \frac{L}{D'^2 R_L}}.$$
 (15)

This model predicts that the positive zero can be shifted to the left-half-plane with leading-edge modulation provided that the following condition is held:

$$R_c C > \frac{L}{D'R_L} \tag{16}$$

This result of the Discrete-Average Model confirms the relationship obtained by analyzing the instantaneous waveforms in (5).

C. SPICE Implementation of Discrete-Average Model

The Discrete-Average Model can be easily implemented in SPICE using a minor modification to the PWM switch model. For trailing-edge modulation, the output

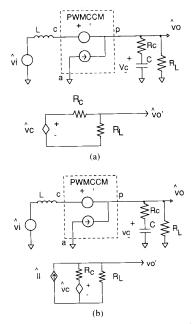


Fig. 4. (a) SPICE implementation of Discrete-Average Model with trailing-edge modulation. Voltage v_o' corresponds to output voltage that control loop will respond to while v_o is average output voltage. (b) SPICE implementation of Discrete-Average Model with leading-edge modulation.

equation is given by

$$v_o = C_1 x = \frac{v_c R_L}{R_L + R_c} \cong v_c. \tag{17}$$

This SPICE implementation is shown in Fig. 4(a). The feature in SPICE known as dynamic multiplication of variables [4] is employed for easy modelling of the PWM block. For leading-edge modulation, the output equation is given by

$$v_o = C_2 x = \frac{i_l R_L R_c}{R_L + R_c} + \frac{v_c R_L}{R_L + R_c} \cong R_c i_l + v_c.$$
 (18)

This SPICE implementation is shown in Fig. 4(b).

Once the feedback loop is closed, proper implementation of the Discrete-Average Model also includes the sampling of the compensation network output. This is described in Section III.

D. Model Comparison

The boost regulator power stage of Fig. 2(a) is modeled in SPICE with 3 techniques, averaging, discrete-averaging with leading-edge modulation, and discrete-averaging with trailing-edge modulation. Fig. 5 shows the control-to-output transfer functions that result from the three models. There are significant differences, especially with regard to the phase. The positive zero is apparent in the averge model and the trailing-edge discrete-average model, by viewing the asymptotic phase response. It is absent from the leading-edge discrete-average model. This boost regulator can, in fact, behave like any one of these

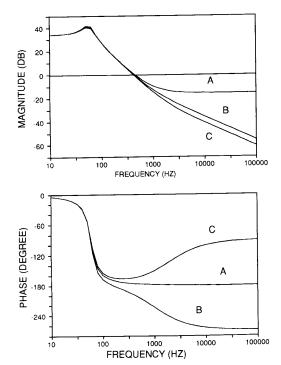


Fig. 5. Control-to-output transfer function of average model (A), Discrete-Average Model with trailing-edge modulation (B), and Discrete-Average Model with leading-edge modulation (C).

three results, depending on the type of modulation and feedback compensation.

III. INDUCTOR CURRENT FEEDBACK WITH LEADING-EDGE MODULATION

A single-loop, leading-edge modulated boost converter has many similarities to a current-mode controlled boost converter. The PWM samples the error signal when the power switch is off. At this time the inductor current is charging the capacitor and feeding the load. The voltage across the capacitor ESR is thus proportional to inductor current. The compensation network amplifies this signal to produce a current sense ramped waveform. This is then compared with the external ramp in the pulse-width-modulator. Recent analysis of current-mode control [5] provides an accurate model of the modulator gain characteristic. Fig. 6 is a block diagram of the system. The gain of the modulator is given by

$$F_m = \frac{1}{(S_n + S_e)T_s}$$
 (19)

where S_n is the slope of the error signal, and S_e is the slope of the external ramp. The current feedback loop in a current-mode controlled regulator also has a frequency dependent element due to the sampling nature of the system. This is given by

$$H_{e}(s) \cong 1 + \frac{s}{\omega_{n}Q_{z}} + \frac{s^{2}}{\omega_{n}^{2}}$$
 (20)

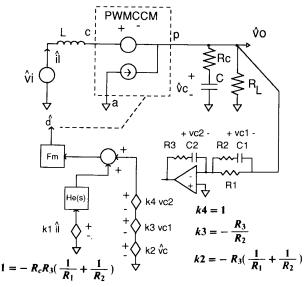


Fig. 6. System block diagram. This representation of power converter and control loop averages all four of system state variables yet samples error signal while the switch is off.

where

$$Q_z = \frac{-2}{\pi}, \qquad \omega_n = \frac{\pi}{T_s}.$$
 (21)

Hence, although the boost regulator positive zero is eliminated from the power stage, two aditional positive zeroes located at one half the switching frequency are introduced due to the sampling nature of the system. These two positive zeroes limit the crossover frequency of the loop gain to below approximately one-fifth of the switching frequency. This is much less constraining, however, than the power stage positive zero which can often limit crossover to below $F_{\rm s}/30$.

Proper implementation of the Discrete-Average Model also includes the sampling of the compensation network output. In Fig. 6 the compensation network has two additional state variables, v_{c1} and v_{c2} . The output equation of this network is given by

$$v_e = \frac{-R_3}{R_2} v_{c1} + v_{c2} - \left(\frac{R_3}{R_1} + \frac{R_3}{R_2}\right) v_0$$
 (22)

where

$$v_o = R_c i_l + v_c. (23)$$

This output equation is implemented with the controlled sources and summing network shown in Fig. 6.

The dependence of the modulator gain on the slope of the error signal acts to mitigate the effects of varying compensator gain or ESR. For example, a decrease in ESR will reduce the gain of the power stage by moving the zero to a higher frequency. However, it will increase the modulator gain by reducing the ripple on the error signal.

IV. PRACTICAL CIRCUIT DESIGN

A. Power Component Selection

A boost converter is designed to the following specifications:

$$V_i = 20 - 25 \text{ V}$$

 $V_o = 30 \text{ V} \pm .3 V_p - p$
 $F_s = 25 \text{ kHz}$
 $P_o = 0 - 50 \text{ W}$

An inductor value of 350 μ H is chosen to allow for a $\pm 15\%$ current ripple at the low line, high load condition. 660 μ F of capacitance with an ESR of 0.075 Ω is used to filter the ripple to the specified value. The condition for elimination of the positive zero is met.

B. Leading-Edge PWM

Most PWM IC's employ trailing-edge modulation. By simply inverting the output pulse, the leading-edge is modulated. To retain negative feedback in the control loop, the error signal is also inverted. Most PWM IC's allow for an adjustable duty cycle maximum limit, a necessity for boost regulators. However, the duty cycle maximum limit becomes a duty cycle minimum once the output is inverted. The duty cycle limit can be externally controlled in several ways. In this implementation, a synchronized signal containing a 50% maximum duty cycle was ANDed with the PWM output.

C. Control Loop Design

A two-pole and two-zero compensator is used in the control loop. The first pole is placed at the origin for dc

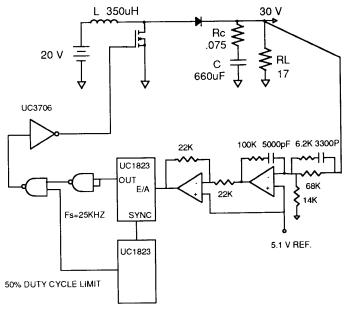


Fig. 7. Schematic diagram of entire power converter circuit.

regulation. The two zeroes are placed to obtain the maximum midband gain and a good phase margin in the loop gain while minimizing the system transient response settling time. The first zero was placed just after the resonant frequency to avoid a conditionally stable system. The second zero was placed at approximately twice the frequency of the first zero. The second pole was placed to cancel the zero in the power stage that has now been moved to the left-half-plane. A wide bandwidth operational amplifier (LM318) was employed to provide the necessary gain at the switching frequency.

Fig. 7 is a schematic diagram of the entire power converter circuit including power stage, PWM and control.

V. System Measurements

A. Loop Gain Measurement

Fig. 8 is a photograph of the steady-state gate drive signal, error signal and output voltage. There is a large discontinuity in the error signal. Conventional loop gain measurement using analog injection techniques will not yield correct results under these circumstances [6]. When an ac signal is injected into the feedback loop, the output voltage and error signal will be both amplitude modulated and duty cycle modulated. The amplitude modulation contains an upper side, corresponding to when the switch is on, and a lower side corresponding to when the switch is off. The crucial gain and phase information is contained in the upper side of the amplitude modulation component. However, the network analyzer tracks all components. The gate drive signal, however, is only duty cycle modulated. This is the only signal in the loop which contains only one modulation component. In order to properly measure the loop gain, digital modulation and measure-

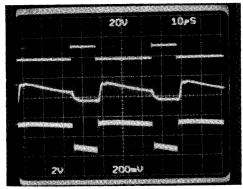


Fig. 8. Photograph of steady state gate drive signal (20 V/Div.), error signal (2 V/Div.), and output voltage waveform (0.2 V/Div. ac). Slope of error signal while switch is off partially determines the gain of modulator.

ment must be employed [6]. Fig. 9 shows the theoretical and experimental loop gain taken at the minimum line and maximum load condition. The theoretical and experimental results are in excellent agreement up to one-half of the switching frequency. The crossover frequency is about 5 kHz, which is one-fifth of the switching frequency. The phase margin is over 60 degrees. Had this been a conventional trailing-edge modulated boost converter, the system would have been unstable. The positive zero would have been at about 3 kHz, causing an additional 45 degrees of phase lag at this frequency. Loop gain crossover would have been constrained to be at about 1 kHz to maintain 60 degrees of phase margin. As with currentmode control, the possibility exists of a subharmonic oscillation. This is evident by what appears to be a small gain margin at half of the switching frequency. The cri-

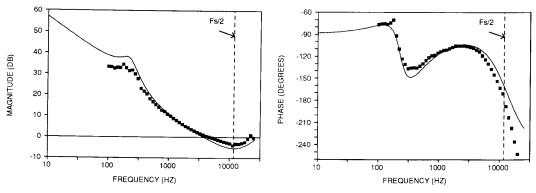


Fig. 9. Theoretical (solid line) and experimental loop gain.

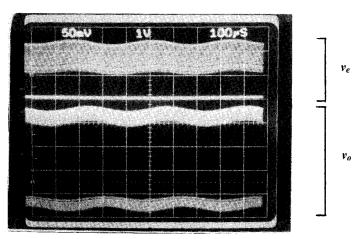


Fig. 10. Photograph of error signal (1 V/Div.) and output voltage (50 mV/Div. ac) with 3 kHz modulation. Both error signal and output voltage waveform appear to be two separate signals due to their discontinuity. Modulation on the upper half of error signal corresponds to modulation on upper half of output voltage. Lower half of error signal is clipped by the feedback amplifier. Phase lag of bottom half of output voltage is significantly greater than top half.

teria for ensuring no subharmonic oscillation is the same criteria that applies to current-mode control. The external ramp in the PWM must have sufficient slope.

B. Measurement of the Control-to-Output Transfer Function

Fig. 10 is a photograph of the error signal and output voltage in the presence of a small-signal external 3 kHz disturbance. The double-sided amplitude modulation of the output voltage is clearly visible. The output voltage appears as two distinct sinusoidal waveforms. The top half of the waveform, corresponding to when the switch is on, has a significantly lower phase lag than the bottom half of the waveform. The switching action between the two sinusoids cannot be resolved in the photograph.

One would like to measure the control-to-output transfer function prior to closing the loop. However, this is not practical in this circumstance. If the error signal and output voltage are placed into the reference and test inputs of a network analyzer, the results will agree with the average model. The network analyzer averages all the com-

ponents of the output voltage switching ripple. This system is unique in that the open loop plant characteristic in fact depends on the feedback control dynamic characteristics. Once the loop is closed, the control-to-output transfer function can be indirectly measured by subtracting the compensator transfer function from the loop gain. This measurement requires care as well, since the compensator input and output are both discontinuous. One possibility, is to employ a sample-and-hold circuit. However, this will introduce phase errors that must be accounted for. The lack of a good measurement procedure for the control-to-output transfer function is one drawback for this technique.

VI. Conclusion

It has been shown how the right-half-plane zero can be eliminated from practical boost converter circuits. The right-half-plane zero is eliminated under the following conditions:

1) Leading-edge modulation must be employed in the pulsewidth modulator.

2) Proper power stage parameter values are necessary:

$$R_c C > \frac{L}{D' R_L}$$

3) The switching ripple must not be integrated by the control loop.

The Discrete Average Model is used to predict this result. It is shown how the Discrete Average Model can be implemented in SPICE using a slight variation of the PWM switch model. This same criterion holds for flyback converter circuits. For flyback converters, the inductance *L*, is the secondary inductance of the flyback transformer.

Conventional analog loop gain measurement is inaccurate due to the pulsating nature of the waveforms. In order to measure the loop gain, digital modulation must be employed.

The theoretical and experimental results indicate high stability margin and wide bandwidth. Loop gain crossover is shown to be much higher than one could ordinarily expect with a conventional trailing-edge modulated boost regulator.

It is shown that leading-edge modulation is very similar to current-mode control in this case. By modulating the leading-edge, the output capacitor current is sampled by sensing the voltage across the ESR. Capacitor current when the switch is off is equal to inductor current minus the load current. By providing an effective feedforward of the load current, this technique ensures excellent load transient response and low output impedance.

There are several disadvantages of this technique. The criterion for shifting the positive zero into the right-half-plane requires a minimum ESR time constant for the output capacitor. Depending on the type of capacitors employed, this may not be practical. In general, aluminum or electrolytic capacitors will probably have a sufficiently long time constant. Film capacitors, ordinarily, cannot be used. An external resistance can be used, however, this will increase the output voltage ripple.

Measurement of the control-to-output transfer function cannot easily be performed. Also, capacitor ESR can often change substantially over temperature. Small changes in the ESR value will not affect the stability margin. This is due to the dependence of the modulator gain on the error signal ripple. However, reduction of the ESR well below the criterion for positive zero elimination will affect system stability. Finally, this technique can be susceptible to noise since the output voltage switching ripple is not filtered in the compensation network.

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