

Power Electronics Notes - D. Perreault

★ (Passive) Power Factor Compensation ^{chap} KSV 3.4.1

Lets focus on the displacement factor component of power factor. For simplicity, lets assume a linear load (e.g. R-L) so that voltages + currents are sinusoidal.

For sinusoidal V, I $P.F = \frac{\langle P \rangle}{V_{rms} I_{rms}} = \cos \phi$

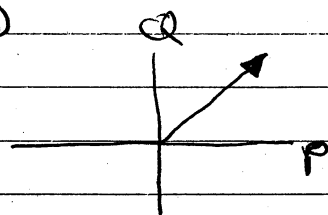
ϕ is the power factor angle
 } leading $\phi < 0$ capacitive
 } lagging $\phi > 0$ inductive

Real Power $P = V_{rms} I_{rms} \cos \phi$

★ Define reactive power as

$Q \triangleq V_{rms} I_{rms} \sin \phi$

In vector form $\vec{S} = P + jQ$



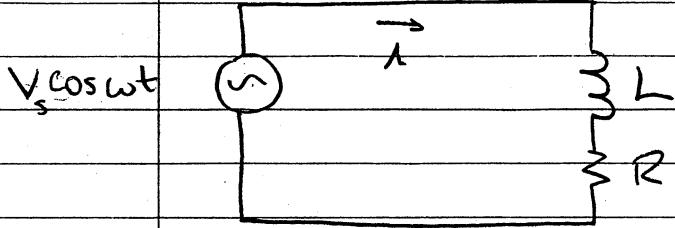
In phasor form $\vec{V}, \vec{I} \rightarrow \vec{S} = \langle V I^* \rangle$

		units
apparent power	$S = \ \vec{S}\ = V_{rms} I_{rms}$	VA
average power	$\text{Re}\{\vec{S}\} = P = V_{rms} I_{rms} \cos \phi$	W
reactive power	$\text{Im}\{\vec{S}\} = Q = V_{rms} I_{rms} \sin \phi$	VAR

we can use these results to help adjust the displacement factor of a system! (make $Q_{net} \rightarrow 0$)

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Suppose we have an R-L load (e.g. an induction machine)

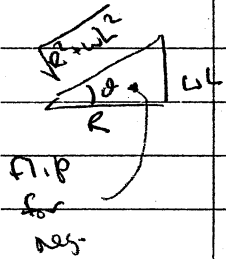


$$i(t) = \frac{V_s}{\sqrt{\omega^2 L^2 + R^2}} \sin(\omega t - \text{ATAN}\left(\frac{\omega L}{R}\right))$$

voltage-current phase $\phi = \text{ATAN}\left(\frac{\omega L}{R}\right)$

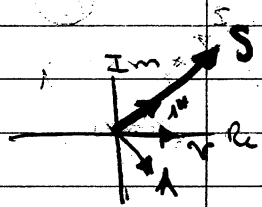
$$\text{P.F.} = \cos\left(\text{ATAN}\left(\frac{\omega L}{R}\right)\right) = \frac{R}{\sqrt{R^2 + \omega L^2}} < 1$$

Voltage-current phase because $S \triangleq VI^*$



we can add some additional reactive load to balance out + give net unity power factor.

$$S = V_{\text{rms}} I_{\text{rms}} = \frac{1}{2} \frac{V_s^2}{\sqrt{\omega^2 L^2 + R^2}}$$

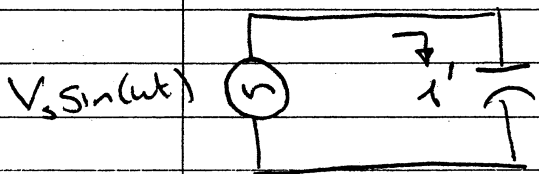


$$P = S \cos \phi = V_{\text{rms}} I_{\text{rms}} \cos \phi = \frac{V_s^2 R}{2(\omega^2 L^2 + R^2)}$$

$$Q = j S \sin \phi = j V_{\text{rms}} I_{\text{rms}} \sin \phi = \frac{j \omega L V_s^2}{2(\omega^2 L^2 + R^2)}$$

so we have real + Reactive power

Suppose we add a capacitor in parallel



$$Z_c = \frac{1}{j\omega C} = \frac{1}{\omega C} e^{-j\pi/2}$$

$$\frac{1}{Z_c} = \omega C e^{j\pi/2} \quad V_{\text{phase}} - I_{\text{phase}} = -90^\circ$$

$$i' = V_s \omega C \sin(\omega t + \pi/2)$$

$$S' = V_{\text{rms}} i_{\text{rms}} = \frac{1}{2} V_s^2 \omega C \quad P' = 0$$

$$Q' = -j \frac{1}{2} V_s^2 \omega C$$