Stabilizing Magamp Control Loop by Using an Inner-Loop Compensation

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Abstract—By using the inner-loop compensation scheme proposed in this paper, the resonance peaking of the open-loop transfer function of a magamp circuit is eliminated. This makes the loop compensation of magamp control much easier. If properly used, the proposed scheme is capable of making the resultant loop gain essentially independent of parameter variation of the saturable reactors.

I. INTRODUCTION

AMAGAMP post regulator is often the preferred choice for many high performance multi-output power supply applications. The major attraction of magamp is that the voltages of a high-current multi-output supply can be independently regulated with efficiency and reliability. Recent papers on this subject reflect the surge of interest in this area [1]–[10].

One of the major tasks in the design of magamp regulators is to compensate the control loop to achieve loop stability and regulation performance. There have been several papers deling with this subject published recently [1]-[3]. In the conventional compensation scheme, the open-loop transfer function is a second order function normally with resonance peaking. To make things worse, the resonance frequency, in some magamps, is sensitive to the parameter variation of the saturable reactor and lineload condition [2]. Compensation of the magamp control circuit, therefore, become rather annoying. The resultant loop performance is sensitive to circuit parameter changes. The major parameter variations are the ESR of the output filter capacitor, the inductance of the choke and the permeability of the saturable reactor.

To rectify this situation, a new compensation scheme is proposed in this paper. By using this new scheme, the open loop transfer function is reduced from second order to first order, therefore the resonance peaking phenomenon is eliminated. If properly designed, the proposed scheme is capable of making the resultant loop gain essentially independent of the power circuit parameters.

In the paper, a review of the problems associated with a conventional compensation scheme is given first. The

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new compensation scheme is then proposed, analyzed and implemented in a circuit. Experimental verification is given and a practical design procedure is illustrated in an example.

II. REVIEW OF CONTROL LOOP BEHAVIOR OF A MAGAMP USING A CONVENTIONAL COMPENSATION SCHEME

Fig. 1 shows a circuit diagram of a PWM-controlled forward converter with a magamp post regulator. Fig. 2(a) shows the circuit diagram of a conventional magamp feedback control circuit with self reset from the regulated output. This paper is focused on this common-used reset scheme. Fig. 2(b) shows the control block diagram of the same circuit. The functional dependence of the small signal transfer functions F_R , F_M and F_F are expressed in (1)–(4):

$$F_{R} \stackrel{i}{=} \frac{\hat{I}_{R}}{\hat{V}_{E}} \begin{pmatrix} \text{control voltage-to-reset current} \\ \text{transfer function} \end{pmatrix}$$
$$= \frac{-R_{B}}{(R_{B} + R_{S})R_{E}} \tag{1}$$

$$F_{M} \stackrel{\circ}{=} \frac{d}{\hat{I}_{R}} \left(\begin{array}{c} \text{reset current-to-duty cycle} \\ \text{transfer function} \end{array} \right)$$
$$= \frac{-0.4\Pi \mu_{M} N^{2} A_{c} f_{s}}{I V + 10^{8}}$$
(2)

where

$$\mu_M = \frac{(\Delta B)^2 f_s}{K_c \cdot P_l \cdot 10^6} \tag{3}$$

where

 $K_c = 1.2$ for Square 80 permalloy

 $K_c = 1.08 \text{ for Magnetic Inc. 2704 metglas}$ $F_F = \frac{\hat{V}_o}{\hat{d}} \text{ (duty cycle-to-output transfer function)}$ $= V_x \left[\frac{1 + SR_CC}{1 + S(R_CC + L/R_c) + S^2LC} \right]$

$$\left|\frac{1}{1 + S(R_C C + L/R_L) + S^2 LC}\right|$$
for continuous mode.

(4)

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Fig. 1. PMW-controlled forward converter with magamp post regulator.





Fig. 2. (a) Magamp control circuit diagram. (b) Control block diagram.

It is to be noted that F_R is a function of the reset circuit resistor values; F_M is a function of saturable reactor parameters, dc operating condition and switching frequency; and F_F is a function of power circuit parameters and d.c. operating condition. For detailed derivation of these transfer functions, readers should refer to [1].

Referring to Fig. 2(b), there are two closed loops in the diagram. The inner-loop consists of F_R , F_M , F_F and the feedback, and the outer loop consists of F_R , F_M , F_F and the error amplifier E/A. The Bode plots of the two open-loop transfer functions are given in Fig. 3, where $F_R F_M F_F$ is the open-loop transfer function of the inner-loop (between points A and B) and $G(=F_R F_M F_F/1 + F_R F_M F_F)$ is the open-loop transfer function of the outer loop (between points C and D with the inner-loop closed). G(s) is



Fig. 3. Bode plot of open loop transfer function of conventional scheme.



Fig. 4. Placement of poles and zeros in conventional compensation scheme.

a second order transfer function with low frequency gain less than 0 dB and the resonance frequency f_{RG} is given by (5), [2]:

$$f_{RG} \cong \frac{1}{2\Pi \sqrt{LC}} \left[1 + F_R F_M F_F(0) \right]^{1/2}.$$
 (5)

It is to be noted that the resonance peaking of G occurs near the Q dB crossover frequency of $F_R F_M F_F$ and the peaking occurs because $F_R F_M F_F$ crossovers 0 dB with -2 slop [2].

Conventional Compensation Scheme

The placement of zeros and poles of a conventional compensation scheme is shown by the dotted line in Fig. 4. The two zeros, f_{Z1} and f_{Z2} , are placed near the resonance peaking frequency f_{RG} and the pole f_{p1} is placed near the capacitor ESR zero f_Z of the power circuit. The second pole f_{p2} is used to suppress switching frequency noise. There are practical difficulties of compensating a magamp circuit this way because of the nature of the two complex poles associated with resonance frequency f_{RG} . First, f_{RG} is highly dependent on saturable reactor parameters and line-load conditions. This is apparent from (5) and the

discussion of functional dependence of transfer functions given earlier in this section. Second, the Q factor of the transfer function G(s), in some cases, is even higher than the Q factor of the original transfer function $F_R F_M F_F$ determined by the power circuit parameters. This makes the peaking of G(s) more pronounced and the changing of the phase angle more rapid near resonance peaking frequency. Both difficulties described above requires conservative placement of compensating zeros to stabilize the system. In doing so, loop gain performance is sacrificed.

III. PROPOSED COMPENSATION SCHEME

To improve the control performance, a new compensation scheme is proposed as follows. Compensation is added to both the F_R block and the E/A block in Fig. 2(b). The former is referred to as inner-loop compensation and the latter as outer-loop compensation. Both are discussed in the following.

Inner-Loop Compensation

The transfer function of the desired inner-loop compensation F'_R is shown by the dotted line in Fig. 5(a). A compensation zero F_{Z1} is placed near resonant frequency f_R of F_F and a compensation pole f_{p1} is placed near capacitor ESR zero of F_F . It is to be noted that the resonance frequency f_R is a function of L and C and is independent of saturable reactor parameters. Therefore, the placement of f_{p1} is relatively straight forward. With the compensation, the magnitude of open inner-loop transfer function $|F_R \cdot F_M F_F|$ is shown by the dotted line in Fig. 5(b). Notice that $|F_R \cdot F_M F_F|$ has a -1 slop at zero dB crossover. This is true if the low frequency gain $|F_R \cdot (0)F_M F_F(0)|$ is much greater than one, which normally is the case.

The open outer-loop transfer function |G'| is shown by the solid line in Fig. 5(b). Notice that G' has essentially become a single-pole transfer function. The pole frequency $f_{PG'}$ can be expressed as follows:

$$f_{PG'} \cong \frac{1}{2\pi \sqrt{LC}} \cdot \frac{F_R F_M F_F(0)}{2} \cdot \left[1 + \sqrt{\frac{4}{F_R F_M F_F(0)}}\right].$$
(6)

It is to be noted that the compensation zero (a real zero) f_{ZI} cannot completely cancel out a resonance pole (complex pole) at f_R . Therefore, $F_R, F_M F_F$ is not exactly a first order transfer function and G' is not either. For theoretical discussion of G' functional behavior and the derivation of (6), one should refer to the Appendix. However, it is concluded from the Appendix that G' is essentially a first-order transfer function and the outer-loop compensation will be done accordingly.

Outer Loop Compensation

Because G'(s) is essentially a first order transfer function, the outer-loop compensation is relatively straight forward. Fig. 6 shows two examples of the placement of compensation transfer functions.



Fig. 5. (a) Placement of pole and zero in proposed inner loop compensation. (b) Magnitude plot of open-loop transfer function with inner loop compensation.



Fig. 6. Placement of poles and zeros in proposed outer loop compensation.

Lead-Lag Compensation: In the case of Fig. 6(a), the desired loop gain crossover frequency f_C is greater than $f_{PG'}$. A compensation zero f_{ZO} is placed near $f_{PG'}$ and a compensation pole f_{PO} is placed for attenuating high frequency noise. From (6), it can be seen that $f_{PG'}$ is a function of saturable reactor parameters and the line-load conditions. Therefore, the placement of f_{ZO} must take the worst condition into consideration similar to the scheme used in a conventional compensation. However, G' in this case is a single-pole transfer function, unlike the G in a conventional scheme in which there is a resonance peaking. Therefore, the placement of f_{ZO} is less critical. Furthermore, because of single-zero compensation as opposed to two-zero compensation as required in a conventional scheme, the low-frequency loop gain of the new scheme usually ends up higher.

Dominant Pole Compensation: In the case of Fig. 6(b), where desired crossover frequency f_C is less than $f_{PG'}$, a dominant pole compensation is used. The main advantage of dominant pole compensation is that the overall loop gain is made essentially independent of saturable reactor parameters and line-load conditions. This is a significant advantage in a high volume production situation. The crossover frequency in this case is lower than that of leadlag compensation. However, it can seen from (6), if the inner open loop gain $F'_R(0)F_MF_F(0)$ is designed large, $f_{PG'}$ is large to begin with and the sacrifice in crossover frequency is minimal.

Circuit Implementation

Fig. 7 shows the circuit implementation of the proposed scheme. The inner loop compensation is achieved by C_E and R_3 . The addition of C_E and R_3 effectively changes the reset circuit transfer function from F_R to F'_R discussed earlier. The outer-loop compensation is achieved by either a lead-lag compensation or a dominant pole compensation in the error amplifier. The determination of the compensation component values is discussed below.

Determination of C_E and R_3 : With the inner-loop compensation, the transfer function F'_R is shown in (7) from which the zero (f_{ZI}) and the pole (f_{PI}) frequency can be found. From the discussion in the last two sections, the inner-loop compensation zero f_{ZI} should be placed at the resonant frequency f_R as indicated by (8). The pole frequency f_{PI} should be placed at capacitor ESR zero frequency f_Z as indicated by (9). Both (8) and (9) will be used later in the design example to determine C_E and R_3 :

$$F'_{R} = \frac{-R_{B}[(R_{E} + R_{3})C_{E}S + 1]}{(R_{B} + R_{S})R_{E}(R_{3}C_{E}S + 1)}$$
(7)

$$\frac{1}{2\pi(R_E + R_3)C_E} = f_{ZI} = f_R = \frac{1}{2\pi\sqrt{LC}}$$
(8)

$$\frac{1}{2\pi R_3 C_E} = f_{PI} = f_Z = \frac{1}{2\pi R_C C}.$$
 (9)



Fig. 7. Circuit implementation of proposed compensation scheme.

Determination of R_f , C_f and C_{hf} (Lead-Lag Compensation) or C_d (Dominant-Pole Compensation): For the leadlag compensation, the outer-loop compensation zero f_{ZO} should be placed at $f_{PG'}$ as indicated by (10) and the compensation pole f_{PO} is placed to attenuate the high frequency noise. Equation (11) shows the functional dependence of f_{PO} on the compensation network parameters. Equation (12) shows the mid-band gain Av of the outerloop compensation network. These equations will be used later in the design example to determine R_f , C_f , C_{hf} and R_I :

$$\frac{1}{2\pi R_f C_f} = f_{ZO} = f_{PG'}$$
(10)

$$\frac{1}{2\pi R_f C_f C_{hf} / (C_f + C_{hf})} = f_{PO}$$
(11)

$$\frac{R_f}{R_1} = Av. \tag{12}$$

For the case of dominant-pole compensation, C_d can be determined by the following equation:

$$C_d = \frac{1}{2\pi f_C R_1}.$$

IV. DESIGN EXAMPLE

Magamp Power Circuit and Circuit Parameters:

$$fs = 50 \text{ Khz}$$

 $L = 190 \text{ uh}$
 $C = 220 \text{ uf}$

 $R_{C} = 0.1 \Omega$ $R_{S} = 1 k\Omega$ $R_{E} = 47 \Omega$ $V_{x} = 72 V$ $V_{O} = 12 V$ $R_{L} = 3 \Omega.$

Saturable Reactor Parameters

N = 38 $A_e = 0.076 \text{ cm}^2$

$$le = 6.18$$
 cm.

Material: Square 80 Permalloy (Mag. Inc. 50B10-1D). Desired loop-gain crossover frequency $f_c = 56$ kHz Find the compensation parameters R_3 , C_E , R_f , C_f and C_{hf} .

Step I: Calculate $F_R F_M F_F(0)$.

(a) From (1),

$$|F_R| = \frac{1 \times 10^3}{(1 + 1) \times 10^3 \cdot 47} = \frac{1}{94}$$

(b) From (2),

$$|F_{M}| = \frac{0.4\pi\mu_{M} \cdot 38^{2} \cdot 0.076 \cdot 50 \times 10^{2}}{6.18 \cdot 72 \times 10^{8}}$$

To find out μ_M , ΔB must be found out first. Using Farady's Law,

$$\Delta B = \frac{V_x \times 10^8}{NA_e f_s} \left(D_Q - \frac{V_O + V_D}{V_x} \right)$$
$$= \frac{72 \times 10^8}{38 \cdot 0.076 \cdot 50 \times 10^3} \left(0.25 - \frac{12 + 1}{72} \right)$$
$$= 3463 \ G.$$

Using $\Delta B/2 = 1734$ G and 50 kHz switching frequency, find core loss density $P_L = 17$ W/lb from core catalog.

Using ΔB and P_L values calculated above, determine μ_M from (3):

$$\mu_M = \frac{(3462)^2 \cdot 50 \times 10^3}{1.2 \cdot (17) \times 10^6} = 29393$$

Therefore,

$$F_M = \frac{0.4\pi \cdot (29393) \cdot 38^2 \cdot 0.076 \cdot 50 \times 10^3}{6.18 \cdot 72 \times 10^8}$$

= 4.6.

(c) From (4),

$$F_F(0) = V_x = 72$$

 $\therefore |F_R F_M F_F(0)| = 1/94 \cdot 4.6 \cdot 72 = 3.55.$ Step II: Determine the inner-loop compensation parameters R_3 and C_F . (a) Placement of compensation zero f_{ZI} , using (8),

$$\frac{1}{2\pi(R_E + R_3)C_E} = \frac{1}{2\pi\sqrt{LC}} = 333 \text{ H}_Z.$$
 (13)

(b) Placement of compensation pole f_{Pl} , using (9),

$$\frac{1}{2\pi R_3 C_E} = \frac{1}{2\pi R_C C} = 1320.$$
(14)

(c) Solve for C_E and R_3 from (13) and (14), noted that $R_E = 47 \ \Omega$ from given specification:

$$C_E = 7.6 \ \mu f$$
 and $R_3 = 15.8 \ \Omega$.

Step III: Determine outer loop compensation parameters.

(a) Calculate |G'(0)| and $f_{PG'}$. From (6),

$$G'(0) = F_{R'}(0)F_M F_F(0) / 1 + F_{R'}(0)F_M F_F(0)$$

= 3.55/1 + 3.55 = 0.78 = -2 db

From (6),

$$f_{PG'} = 333 \cdot \frac{3.55}{2} \left[1 + \sqrt{\frac{4}{3.55}} \right] = 1434.$$

(b) Placement of compensation zero f_{ZO} . Using (10),

$$\frac{1}{2\pi R_f C_f} = 1434.$$
(15)

(c) Placement of compensation pole f_{PO} . f_{PO} is placed to attenuate the switching-frequency noise. It should be equal to or greater than the desired loop-gain crossover f_C but should be significantly smaller than switching frequency. In this example, 5 kHz is selected. Using (11),

$$\frac{1}{2\pi R_f \left(\frac{C_f \cdot C_{hf}}{C_f + C_{hf}}\right)} = 5000.$$
(16)

(d) Sketch the approximated G'(s) using the results of Step III-(a).

(e) Sketch the desired transfer function Fcomp. Using the corner frequencies obtained from Step III-(b) and (c) and set |Fcomp(f = 5 kHz)| = |G'(f = 5 kHz)| in order to achieve the desired loop-gain crossover-hyphen frequency of 5 kHz. The result is similar to Fig. 6(a).

(f) From the F comp obtained in the last step, obtain mid-frequency gain Av = 14 dB. Using (12), and set Av = 14 dB,

$$\frac{R_f}{R_1} = 14 \text{ dB}.$$

(g) Determine R_1 and R_2 . Assume the reference voltage of the operational amplifier is 2.5 V.

From the consideration of the noise immunity and power dissipation in the two resistors R_1 and R_2 , R_2 is selected to be 2.5 K Ω . R_1 can then be determined, by voltage divider equation, to be 9.5 K Ω .



Fig. 8. Comparison of the predicted and measured G' function and $G'F_{comp}$ function. (a) Neglecting phase delay in F_m . (b) Incorporating phase delay in F_M .

(h) Solve for R_f , C_{hf} . From (17),

$$R_f = 64 \text{ K}\Omega$$

From (15) and (16),

$$C_f = 7.5 \text{ nF}$$
 and $C_{hf} = 5.37 \text{ pF}$.

Experimental Verification and Discussion

Fig. 8(a) shows the comparion between the predicted and the measured G' function and the loop gain G'Fcomp. There is a good agreement between the two. Generally speaking, when the frequency exceeds 3 kHz, however, phase angle deviation becomes pronounced. This is due to the fact that the phase delay associated with the transfer function F_M is neglected in this paper. The phase delay ϕ_D associated with F_M can be approximated by the following relationship [9].

$$\phi_D(\text{in radian}) = -(2D' + \alpha)\frac{f}{f_s}$$

where D' is the off duty cycle of the diode D_1 and α is factor associated with reactor resetting source. It ranges between 0 and 1. $\alpha = 0$ for a perfect current resetting



Fig. 9. Predicted loop-gain changes due to saturable reactor variation ($R_c = 0.1 \Omega$). (a) Conventional compensation. (b) Inner loop compensation with lead-lag outer-loop compensation.

source and $\alpha = 1$ for a perfect voltage resetting source. In this example, $D' = 1 - V_O/V_x = 0.83$ and α is selected to be 0.2 because this number best fits the experimental results. Fig. 8(b) shows the resultant comparison of predicted values and measured values when the phase delay is taken into consideration. In Figs. 9 to 11, phase delay is also incorporated in the model. For frequency less than one tenth of the switching frequency, however, the phase delay can be ignored without loss of accuracy.

Comparison of Conventional Compensation Scheme and Inner-Loop Compensation Scheme: Fig. 9 shows the resultant loop gain transfer function using both the conventional compensation scheme and the inner-loop compensation scheme. The circuit parameters used for the solid curves are identical to those used in the Design Example. When the low frequency gain $F_{R'}(0)F_MF_F(0)$ is increased to 8.75, the loop gain variation is indicated by the dotted curve. As can be seen from this figure, the inner-loop compensation scheme gives smaller loop-gain variation as $F_{R'}(0)F_MF_F(0)$ changes. Among the parameters that may cause $F_{R'}(0)F_MF_F(0)$ change, the reactor average permeability μ_M is most susceptible to unit-to-unit



Fig. 10. Predicted loop-gain changes due to saturable reactors variation ($R_c = 0.03 \ \Omega$). (a) Conventional compensation. (b) Inner-loop compensation with lead-lag outer-loop compensation.

variation. In this case, the performance difference between the two compensation schemes is still not very striking. As capacitor ESR varies, the effect becomes more pronounced as shown below.

Effect of Capacitor ESR: Fig. 10 shows similar comparison as Fig. 9 but the filter capacitor ESR value is reduced from 0.1 Ω to 0.03 Ω . The advantages of using the inner-loop compensation are even more pronounced. This is because in the conventional scheme, the capacitor ESR zero in the loop gain function is farther away from the two resonance poles, which makes the resonance effect more pronounced. The phase angle approaches- 180° before the ESR zero tends to pull it back to- 90° . In the inner-loop compensation scheme, however, there is a compensation zero to dilute the effect of the resonance poles regardless of the ESR zero and consequently ESR zero has relatively little effect on the resultant loop gain performance.

Dominant-Pole-Compensation: Using the same circuit parameters and same crossover frequency requirements as



the Design Example, one should not use dominant pole compensation. This is because $f_{PG'}$ (= 1434 Hz) is much less than f_C (= 5 kHz). If the inner-loop gain is increased to make $F_{R'}(0) F_M F_F(0) = 15$, then $f_{PG} \approx 5$ kHz according to (6). Under this condition, a dominant-pole compensation can be used without risking system instability. Fig. 10 shows the resultant loop gain transfer functions. As can be seen from the figure, frequency less than f_C , the loop gain is essentially independent of parameter variation of the saturable reactor. In other words, the loopgain crossover frequency is essentially independent of power circuit parameter variation.

V. CONCLUSION

Using the inner-loop compensation scheme described in this paper, the order of the open-loop transfer function of a magamp control circuit is essentially reduced from two to one for a self-reset scheme. The problem normally associated with compensating a control transfer function with resonance peaking is therefore eliminated. Moreover, if the inner loop gain is designed high enough, the closed-loop gain can be insensitive to the variation of power circuit parameters such as saturable ractor permeability and capacitor ESR, which is a very desirable feature in a high-volume production situation.

A design example is given to illustrate the step-by-step design procedure for a practical magamp control circuit. The results are verified by loop gain measurements.

VI. NOMENCLATURE

 A_e Effective cross-section area of the saturable reactor (cm²). ΔB Flux density swing of the saturable reactor (G).

С Capacitance of output filter capacitor (F). C_E Inner loop compensation capacitance (F). C_f, C_{hf}, C_d Outer loop compensation capacitance (F). Small signal variation of the duty cycle of saturable reactor (dimensionless). D_{Q} Main transistor duty cycle (dimensionless). Frequency (s^{-1}) . Fcomp Outer loop compensation transfer function (dimensionless). f_{C1} 0 db crossover frequency of $F_{R'}F_MF_F(s^-)$. F_F Duty cycle-to-output transfer function (V). F_M Reset current-to-duty cycle transfer function or modulator gain of the saturable reactor (A^{-1}) . Pole frequency of $G(s^{-1})$ f_{PG} Pole frequency of G' (s⁻ h. $f_{PG'}$ Inner loop compensation pole frequency f_{PI} $(s^{-1}).$ Outer loop compensation pole frequency fpo $(s^{-1}).$ Inner loop compensation zero frequency fzi $(s^{-1}).$ Outer loop compensation zero frequency fzo $(s^{-1}).$ Resonant frequency of F_F . f_R F_R Control voltage-to-reset current transfer function (mho). $F_{R'}$ Control voltage-to-reset current transfer with inner loop compensated (mho). Resonant frequency of transfer function f_{RG} $F_{R'}F_{M}F_{F}/(1 + F_{R'}F_{M}F_{F})$ (s⁻¹). G $F_R F_M F_F / (1 + F_R F_M F_F)$ (dimensionless). G'

 $F_{R'}F_MF_F/(1 + F_{R'}F_MF_F)$ (dimensionless).

K_C	A factor for calculating μ_M .
l_e	Mean length of magnetic path (cm).
L	Inductance value of output filter inductor
	(H).
Ν	Number of turns of the saturable reactor
	(dimensionless).
P_L	Core loss density (W/lb) .
R_B	Voltage divider resistance of reset circuit
	(Ω).
R_C	Capacitor ESR (Ω).
R_3	Inner loop compensation resistance (Ω).
R_E	Emitter resistance of reset circuit (Ω) .
R_{f}	Outer loop compensation resistance (Ω).
R_L	Load resistance (Ω) .
R_S	Voltage divider resistance of reset circuit
	$(\Omega).$
μ_M	Average permeability of the saturable re-
	actor (G/Oe) .
V_D	Diode voltage drop (V).
\hat{V}_E	Small signal error voltage (V).
V_o	dc output voltage (V).
Ŷ _O	Small signal output voltage (V).
V_x	Transformer secondary voltage when the
	main transistor is conducting (V).

Appendix

A. Behavior of the G' Function

In this section, the behavior of the G' function is discussed using phasor diagrams. Fig. 12(a) shows the general shapes of several transfer functions involved from which G' function will be derived. Fig. 12(b) shows the resultant G' function. There are two assumptions made in this discussion: 1) $F_{R'}(0)F_MF_F(0) >> 1$, and 2) $f_{C1} >> f_R$. Since $G' = F_{R'}F_MF_F/(1 + F_{R'}F_MF_F)$ and $F_{R'}F_MF_F$ is a phasor, the behavior of G' is investigated by using phase diagrams as follows:

 $f \ll f_R$:

Since $F_R F_M F_F >> 1$ and $\angle F_R F_M F_F \approx 0^\circ$, |G'| is slightly less than 1, and $\angle G'$ is very small.

f is slightly less than f_R :

From Fig. 12(a), $0^{\circ} < (\angle F_{R'}F_MF_F) < 45^{\circ}$. Therefore from Fig. 13(a), $0^{\circ} < (\angle G') < 45^{\circ}$, and |G'| is slightly less than 1. Normally, $\angle G$ is much smaller than 45° ;

f is slightly larger than f_R :

From Fig. 12(a), $0^{\circ} > (F_R \cdot F_M F_F) > -135^{\circ}$. Therefore, from Fig. 13(b), |G'| can be greater or less than 1 depending upon $\angle F_R F_M F_F$ value. But in either case, |G'|is very close to 1, and $0^{\circ} > (\angle G') > -45^{\circ}$. Normally, $|\angle G'|$ is much smaller than 45°;

 $f = f_{C1}$:

From Fig. 12(a), $-90^{\circ} > (\angle F_R \cdot F_M F_F) > -135^{\circ}$, depending on the relative magnitude of f_{C1} and f_R . Therefore, from Fig. 13(c) $-45^{\circ} > (\angle G') > -67.5^{\circ}$ and $(1/\sqrt{2}) < |G'| < a$ number slightly greater than 1. Because $f_{C1} >> f_R$, $\angle G'$ is normally closer to -45° ; $f >> f_C1$:

For this frequency range, $F_{R'}F_MF_F \ll 1$ and



Fig. 12. (a) Bode plots of $F_{R'}F_MF_{F'}$ (b) Bode plot of G'.



Fig. 13. Phasor diagrams for studying behavior of G' function (a) f is slightly less than f_{R} . (b) f is slightly greater than f_{R} . (c) f is equal to f_{C1} .

 $< F_{R'}F_MF_F \approx 90^\circ$. Therefore, $|G'| \cong F_{R'}F_MF_F$ and $\angle G' \approx -90^\circ$.

From the above discussion, it can be seen that G'(s) can be approximated by a single-pole transfer function

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with pole locating at f_{C1} , i.e., $f_{PG'} \approx f_{C1}$. The plot of G' is shown in Fig. 12(b).

B. Derivation of (6)

The inner-loop transfer function after (inner-loop) compensation can be expressed as follows:

$$F_{R'}F_{M}F_{F} = \frac{K\left(\frac{s}{\omega_{o}} + 1\right)}{\frac{s^{2}}{\omega_{o}^{2}} + \frac{1}{Q}\frac{s}{\omega_{o}} + 1}$$

where K is equal to $F_{R'}(0)F_MF_F(0)$, the low frequency gain. K is assumed to be much greater than 1. Q is the quality factor and is assumed to be greater than 1, and ω_o $= 1/\sqrt{LC}$. From the derivation in Part A, $f_{PG'} \cong f_{C1}$. To find out f_{C1} , one can proceed as follows:

At $f = f_{C1}$, $F_{R'}F_MF_F = 0$ dB = 1. Therefore, set

$$F_{R'}F_MF_F = \frac{K\left(\frac{s}{\omega_o} + 1\right)}{\frac{s^2}{\omega_o^2} + \frac{1}{Q}\frac{s}{\omega_o} + 1} = 1$$

and solve for the roots s_1 , and s_2 .

$$s_1, s_2 = \frac{\left(\frac{1}{Q\omega_o} - \frac{K}{\omega_o}\right) \pm \sqrt{\left(\frac{1}{Q\omega_o} - \frac{K}{\omega_o}\right) - \frac{4(1-K)}{\omega_o}}}{\frac{2}{\omega_o^2}}.$$

Since Q > 1 and K >> 1 and the root must be positive,

$$s_1 \cong \frac{\omega_o K}{2} \left[1 + \sqrt{1 + 4/K} \right]$$

Therefore,

$$f_{PG'} = f_{C1} = \frac{s_1}{2\pi}$$

= $\frac{1}{2\pi \sqrt{LC}} \cdot \frac{F_{R'}(0)F_M F_F(0)}{2}$
 $\cdot \left[1 + \sqrt{1 + \frac{4}{F_{R'}(0)F_M F_F(0)}}\right]$

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